



ILMATIETEEN LAITOS  
METEOROLOGISKA INSTITUTET  
FINNISH METEOROLOGICAL INSTITUTE

# Data assimilation over lakes

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# Introduction

Why DA for lakes is needed?

Model errors may be large.

Observations exist: in-situ, satellite - MODIS

New data are coming: ESA-funded projects

ArcLake - ATSR, coarse resolution, 500 large lakes

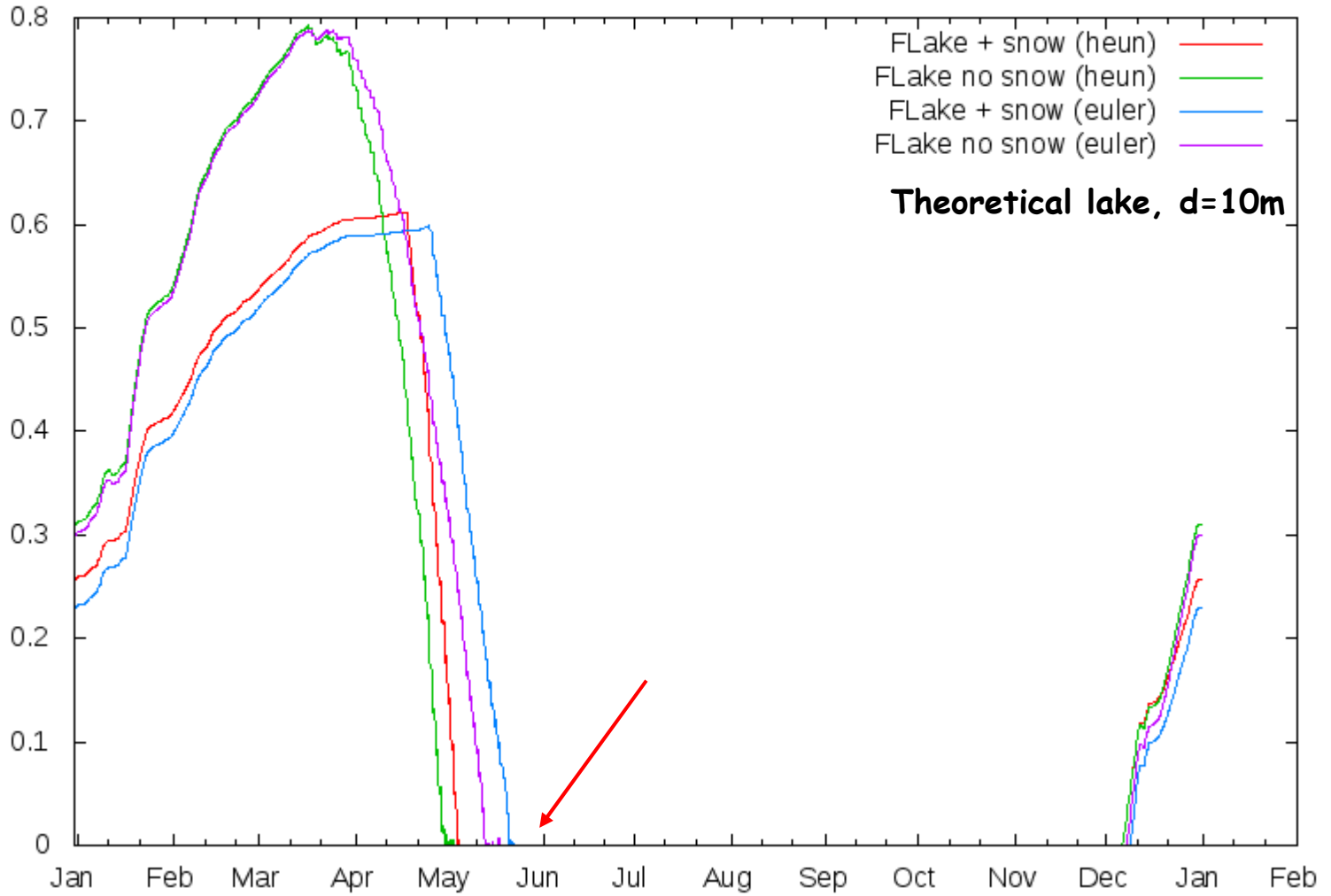
North Hydrology - ATSR, 1 km resolution, all lakes in Nordic domain



### GDAS forcing, different integration schemes

h\_ice  
30E 60N

By Yurii Batrak





# Lake observations

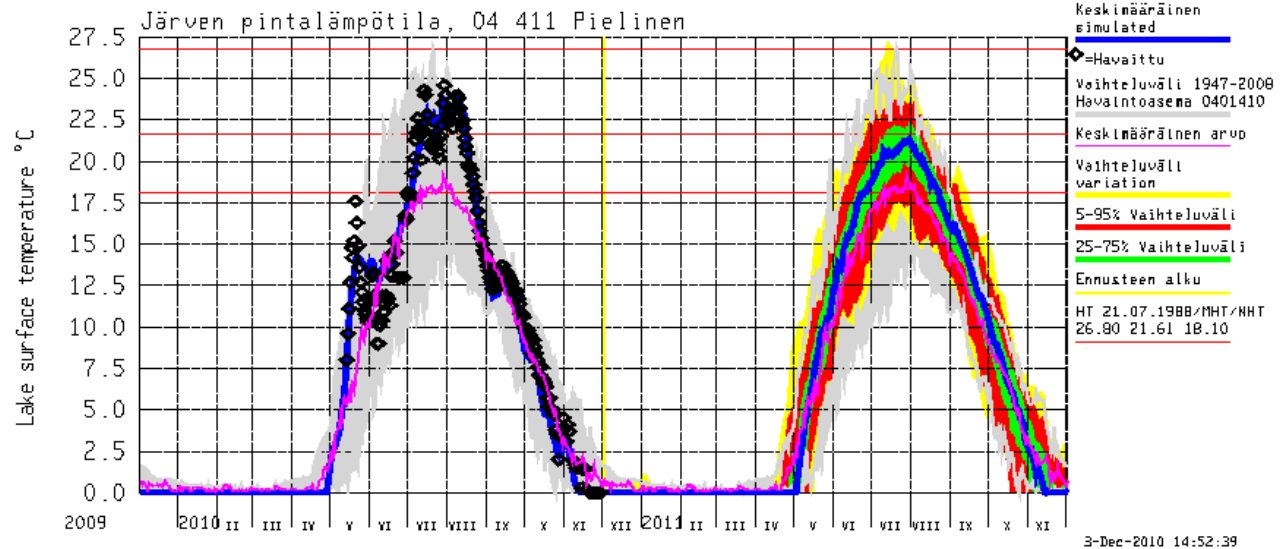
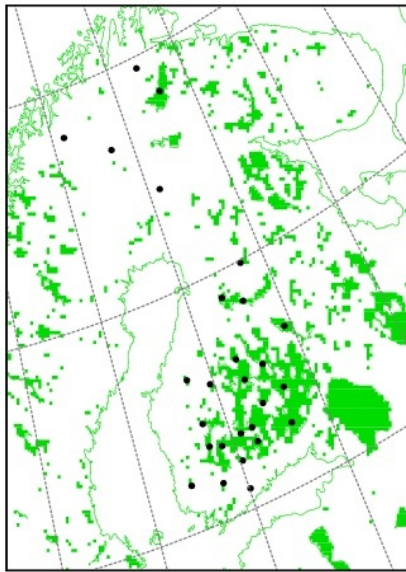
What we observe and can assimilate:

- Temperature - LST
- Ice cover
  - very important!
  - ice/no ice, ice fraction, ice thickness (?), snow on ice (?)

In general, both fields are discontinuous in space and time



# Lake observations



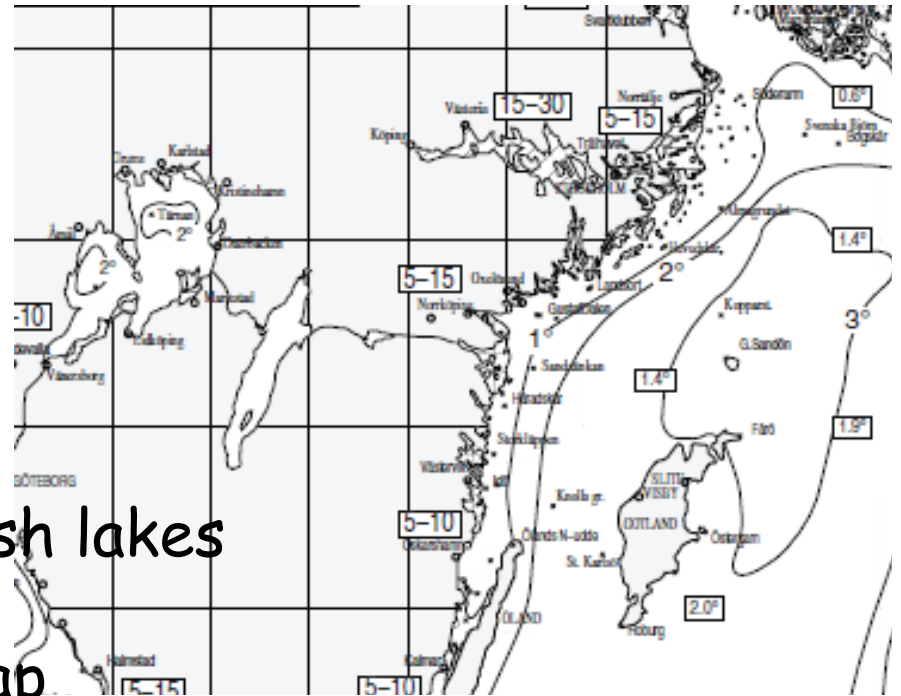
Lake surface temperature  
*in-situ* observations over 27 lakes in Finland



# Lake observations

Satellite-based, gridded

water temperature obs for  
the Baltic Sea and large Swedish lakes  
Lake Vänern and Lake Vettern,  
based on the operational ice map  
by FMI

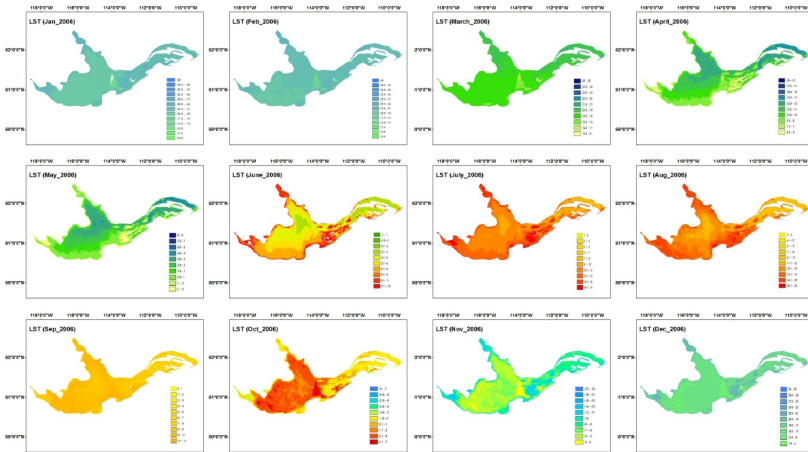


[http://www.itameriportaali.fi/en/itamerinyt/en\\_GB/jaatilanne/](http://www.itameriportaali.fi/en/itamerinyt/en_GB/jaatilanne/)



# Lake observations

## LST, Great Slave Lake



remote sensing  
observations  
- MODIS 1 km resolution,  
clear sky conditions.

## Quality of remote sensing observations:

- Undetected clouds
- Skin temperature
- Lake mask
- Spring ice

Preprocessing and quality control is needed





# Lake data assimilation: overlook and methods

More similar to Land surface than to oceanographic DA

For the coupled system lake/atmosphere (3D) we need:

- To spread information in vertical (inside FLake) (1D)
- To spread information in horizontal (2D)
  - from in-situ obs into the model grid
  - from the image grid to the model grid



# Lake data assimilation: overlook and methods

To spread information in horizontal

- for LST and fraction of ice, use OI as for SST, but with the dependency of structure functions on the difference in lake depth and elevation?
- for remote sensing data: thinning, super-observations by averaging, lake masks consistency problem



# Lake model FLake from DA point of view

FLake - a bulk lake model 1D (0D)

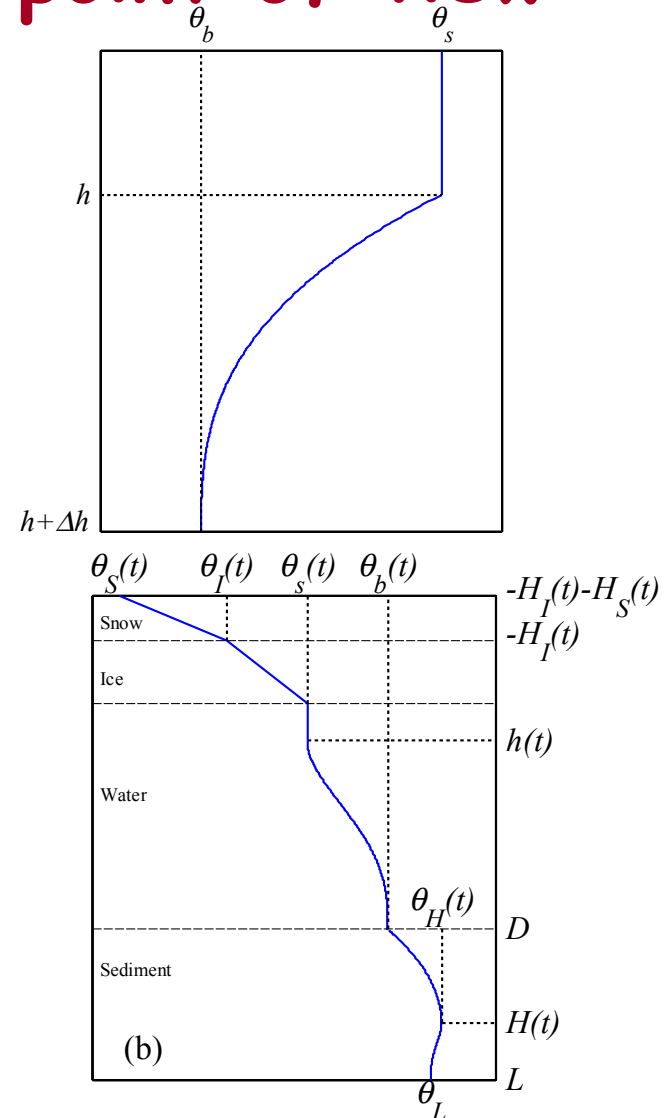
based on two-layer parametric representation of the temperature profile and self-similarity concept

$\theta_s(t)$  - mixed layer temperature

$h(t)$  - mixed layer depth

$\theta_b(t)$  - bottom temperature

$D = h + \Delta h$  - lake depth.





# Lake model FLake from DA point of view

## Prognostic equations

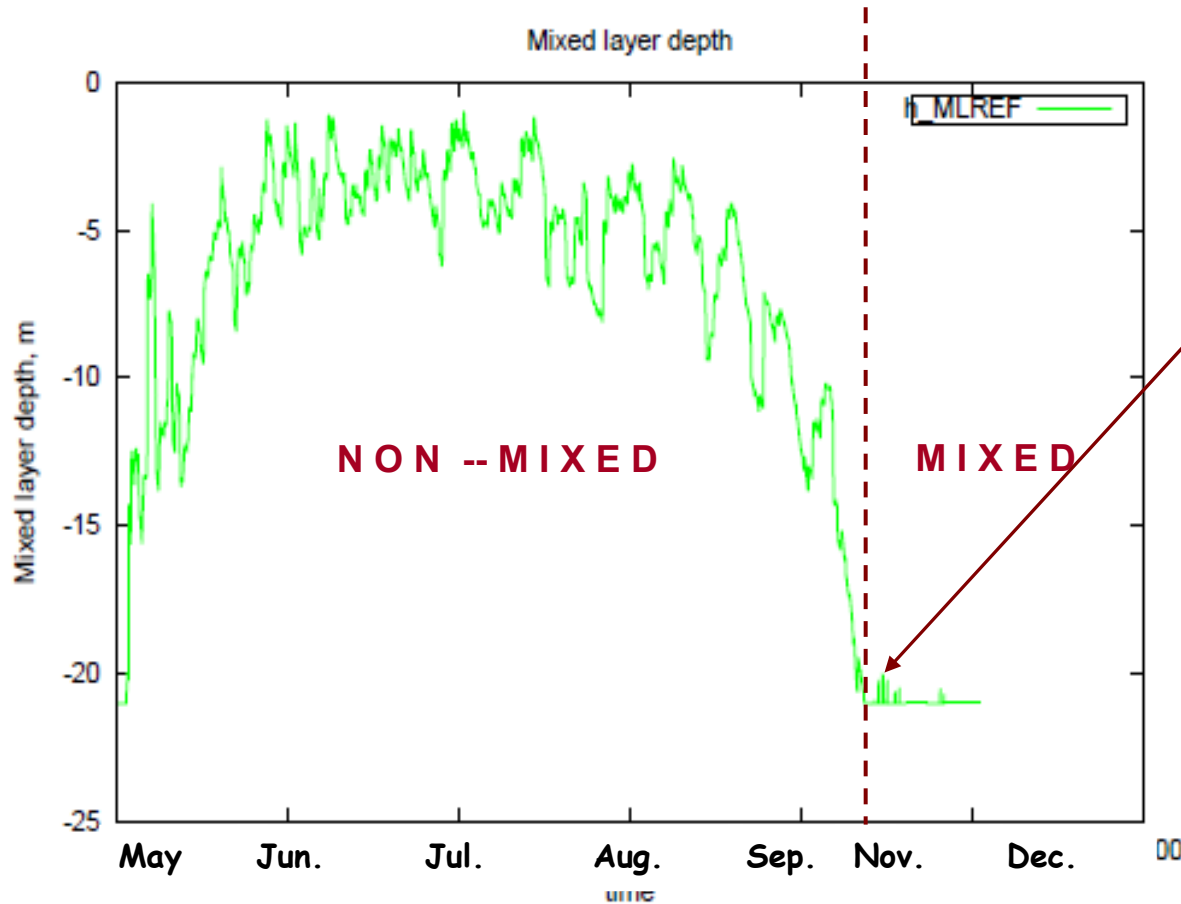
- for the mean water temperature
- for the bottom temperature
- for the mixed layer depth (in the cases of neutral stratification and convection)
- for the shape factor

## Diagnostic equation

- for the mixed layer (surface) temperature



# Lake model FLake from DA point of view



- jumps  
between regimes -  
discontinuities  
in the model

- fast variables  
and slow  
variables

- model biases?



# EKF for FLake to assimilate LST

non-mixed regime

$$\mathbf{x} = \begin{bmatrix} \bar{T} \\ T_b \\ h \\ C_T \end{bmatrix} \quad \text{state vector}$$

obs vector

$$\mathbf{y} = [T_s]$$

obs operator  $H(\mathbf{X})$

$$T_s = \left( 1 - C_T \left( 1 - \frac{h}{D} \right) \right)^{-1} \left( \bar{T} - \left( 1 - \frac{h}{D} \right) T_b \right)$$



# EKF for FLake to assimilate LST

mixed regime

state vector

$$\mathbf{x} = [\bar{T}]$$

obs vector

$$\mathbf{y} = [T_s]$$

obs operator  $H(\mathbf{X})$

$$T_s = \bar{T}$$



# EKF for FLake to assimilate LST

non-mixed regime

Linearised obs operator:

$$\mathbf{H} = \begin{bmatrix} 1 & C_T(\bar{T} - T_b) & -C_T\eta & \eta(\bar{T} - T_b) \\ 1 - C_T\eta & (1 - C_T\eta)^2 & (1 - C_T\eta) & (1 - C_T\eta) \end{bmatrix}$$

mixed regime

Linearised obs operator:

$$\mathbf{H} = 1$$

$$\eta = 1 - \frac{h}{D}$$





# EKF for FLake to assimilate LST

non-mixed regime, mixed regime

Jacobians matrix for FLake:

$$\mathbf{M} = \frac{\partial x_i^t}{\partial x_j^0}$$

No DA when jumping between regimes to handle discontinuities



## EKF for FLake to assimilate LST

$$\mathbf{x}_B = M(\mathbf{x}_A)$$

$$\mathbf{B} = \mathbf{MAM}^T + \mathbf{Q}$$

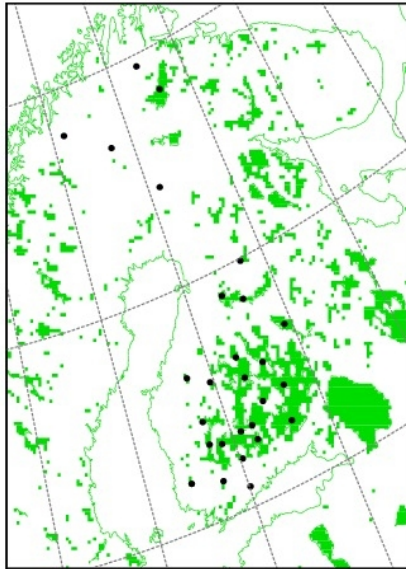
$$\mathbf{K} = \mathbf{BH}^T (\mathbf{HBH}^T + \mathbf{R})^{-1}$$

$$\mathbf{x}_A = \mathbf{x}_B + \mathbf{K}(\mathbf{y} - H(\mathbf{x}_B))$$

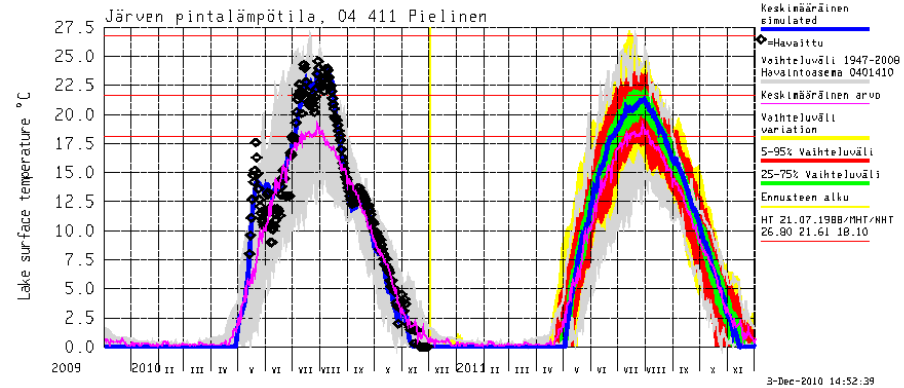
$$\mathbf{A} = (\mathbf{I} - \mathbf{KH})\mathbf{B}$$



# Assimilation of SYKE obs



Lake surface temperature  
*operational in-situ* obs  
over 27 lakes in Finland



No LST obs during ice period:

if LST="no data" value,  
it may be ice!

if LST = "no data", stop DA!  
=> ice is considered indirectly



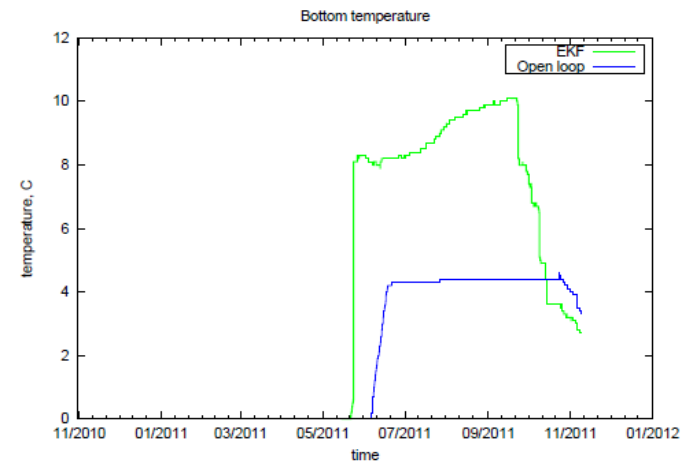
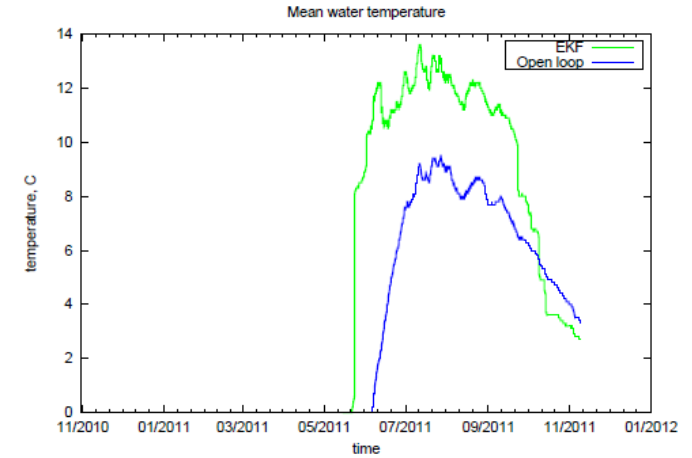
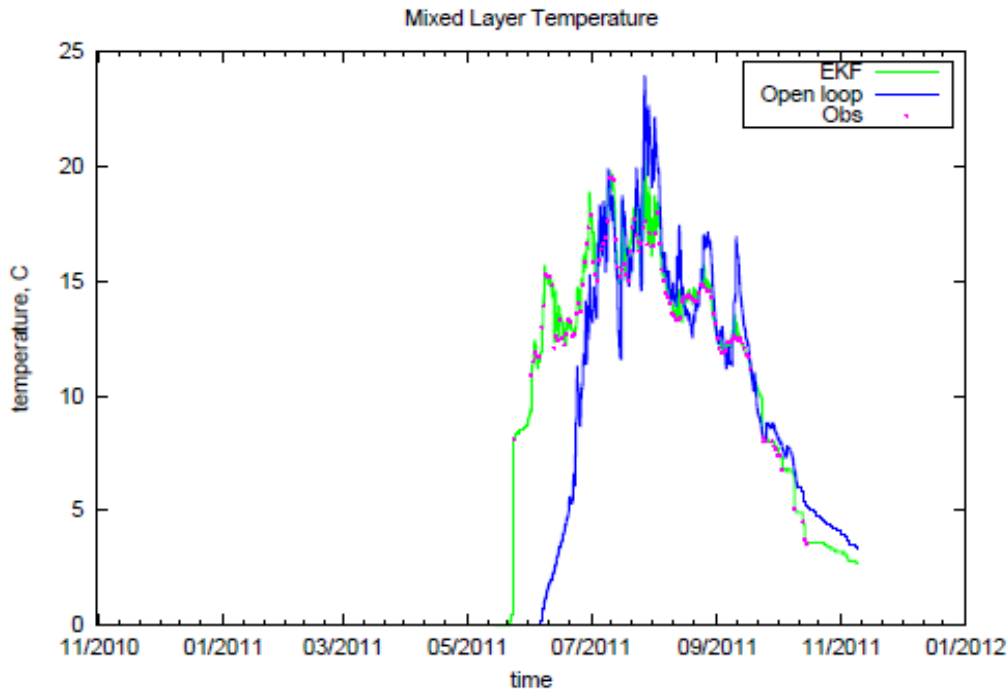
# Assimilation of SYKE obs

- 27 lakes
- 3.11.2010-10.11.2011
- FLake offline
- Forcing from operational HIRLAM forecasts
- Obs at 8.00 UTC
- Analysis at 6.00 UTC
- Assimilation window - 2h
- Assimilation cycle - 24 hours



# Assimilation of SYKE obs

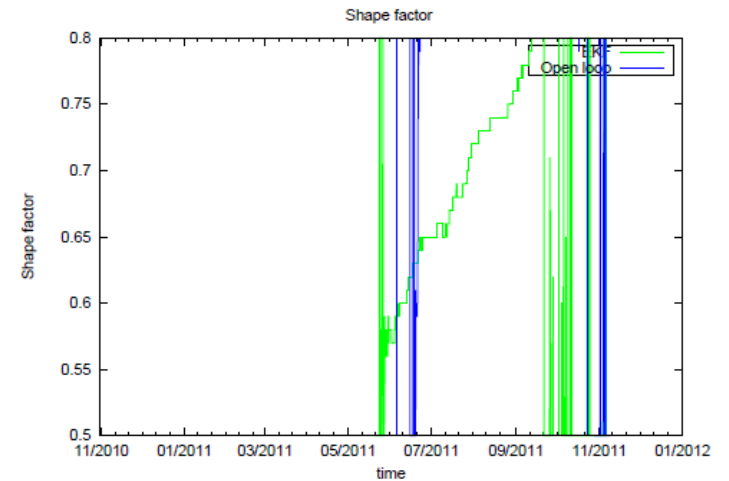
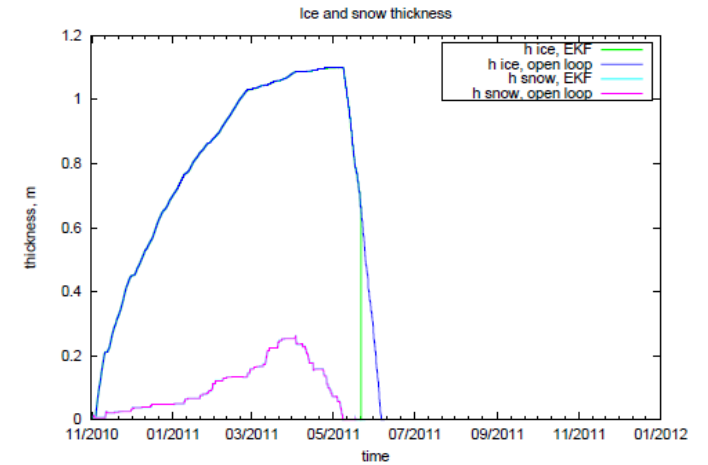
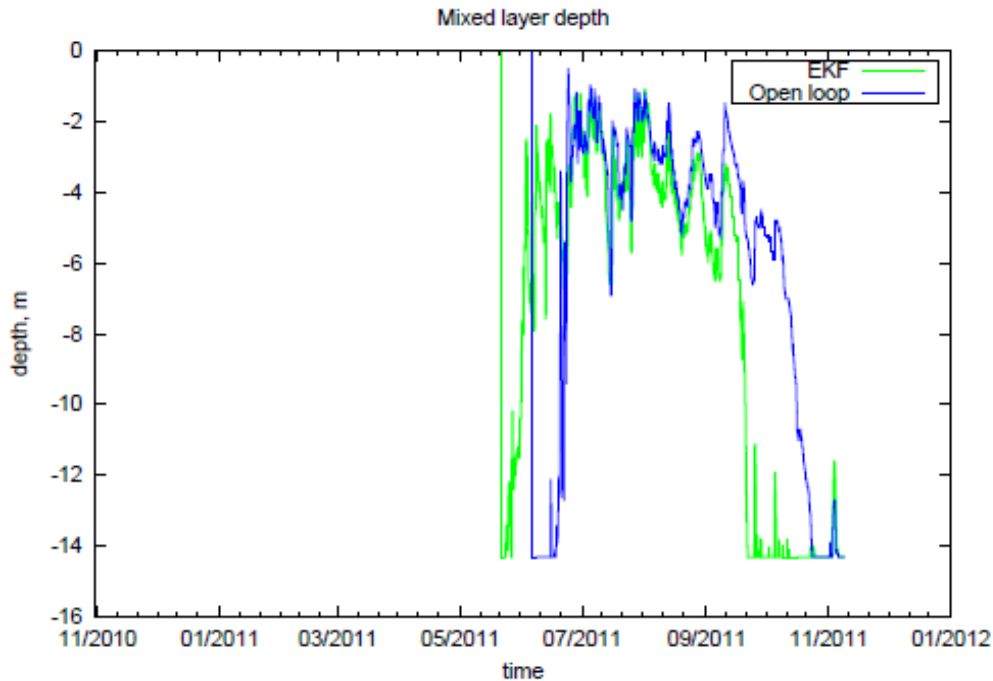
Lake Iänri, 14m





# Assimilation of SYKE obs

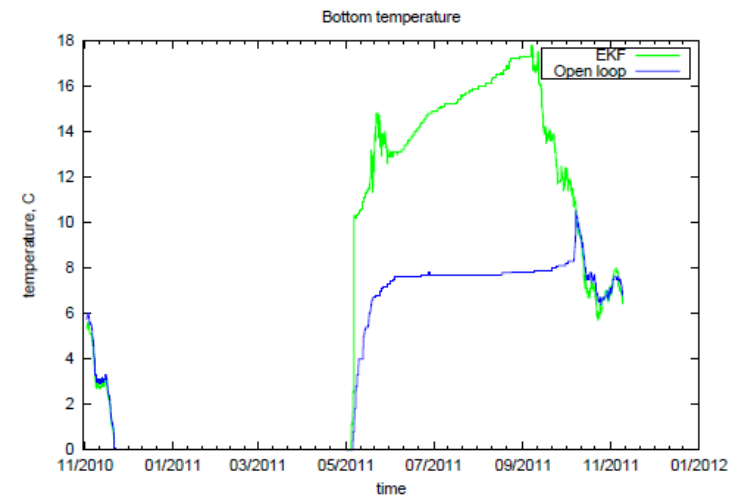
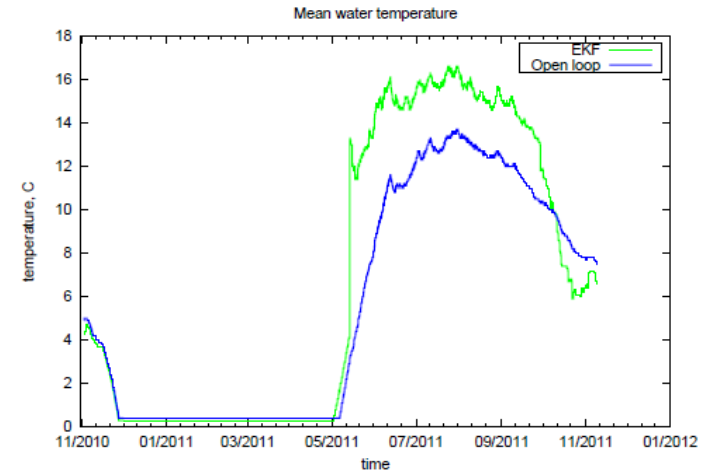
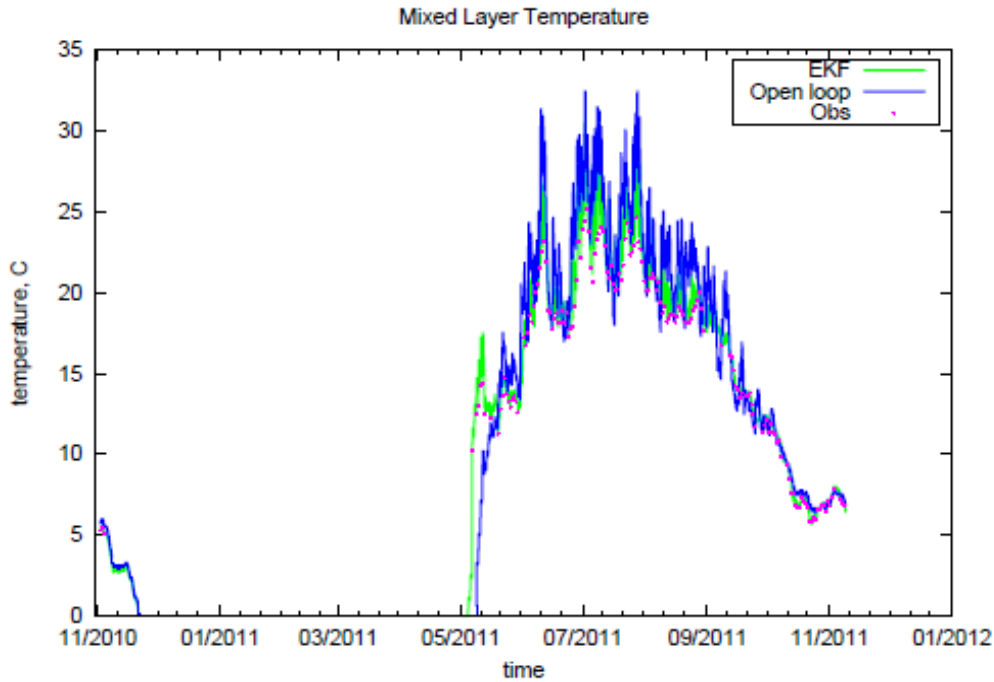
Lake Iänri, 14m





# Assimilation of SYKE obs

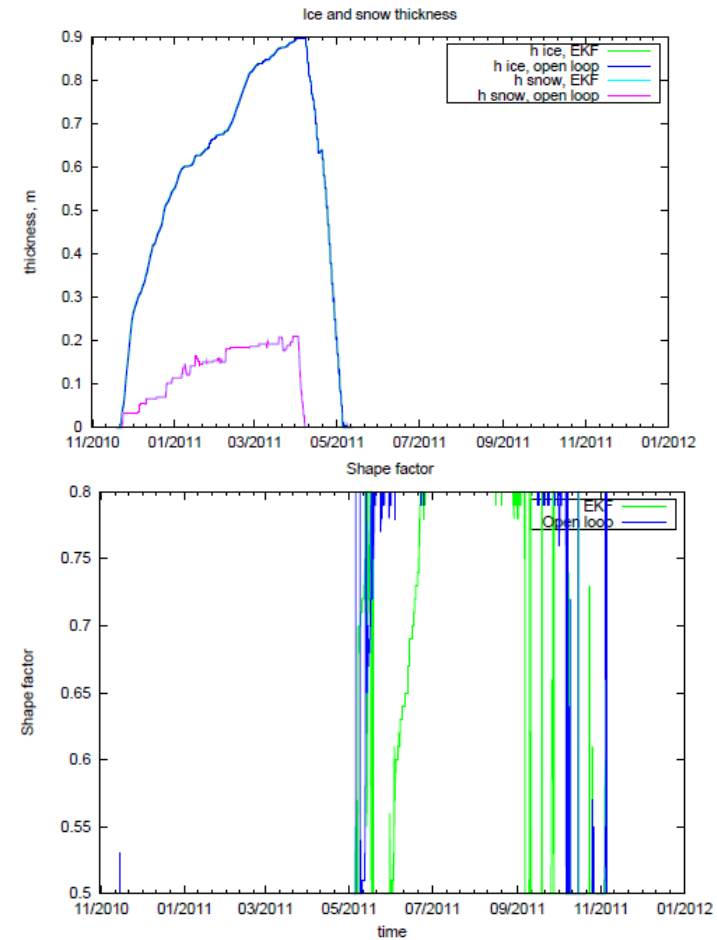
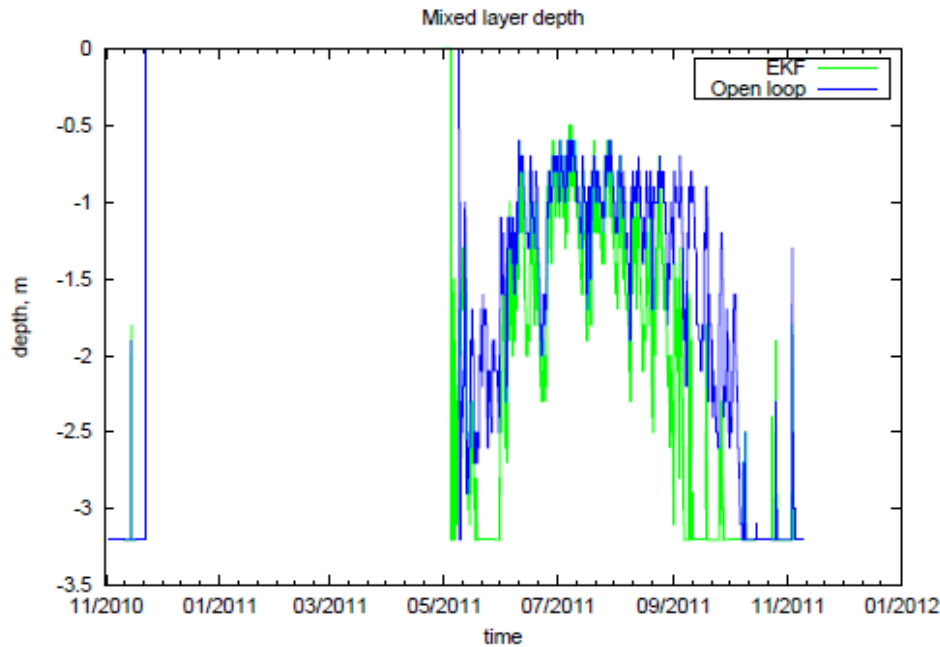
## Lake Tuusula, 3m





# Assimilation of SYKE obs

## Lake Tuusula, 3m



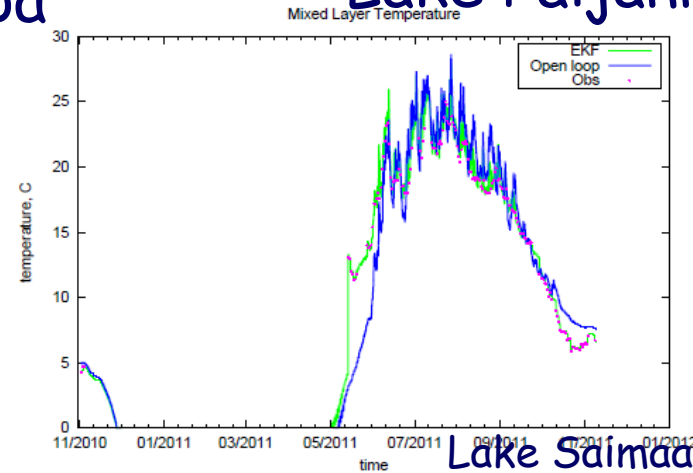
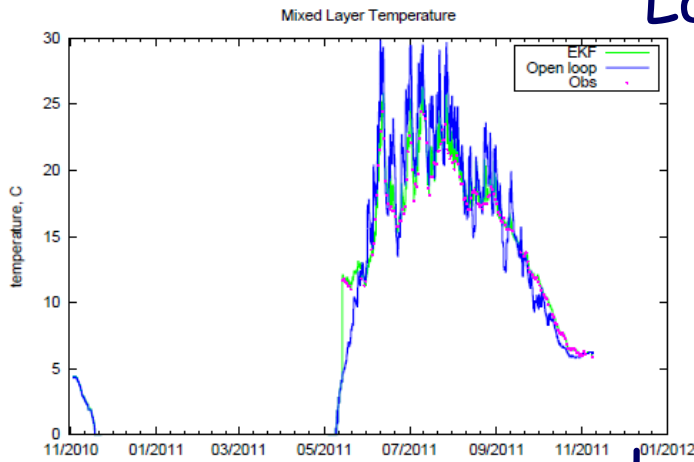




# Assimilation of SYKE obs

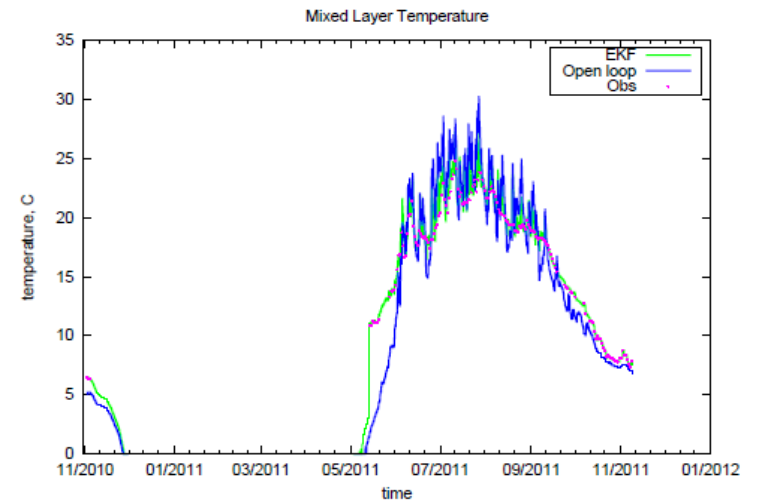
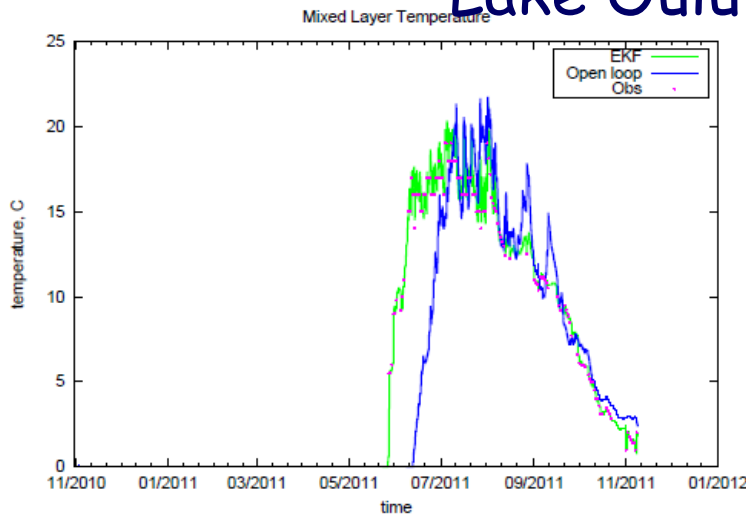
Lake Lappa

Lake Paijanne



Lake Oulu

Lake Saimaa





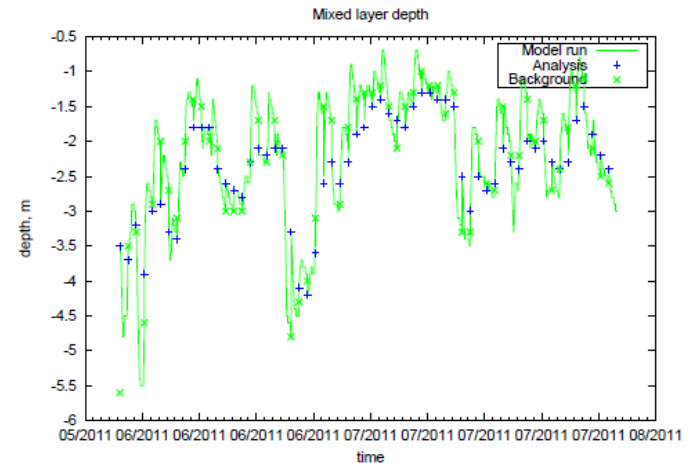
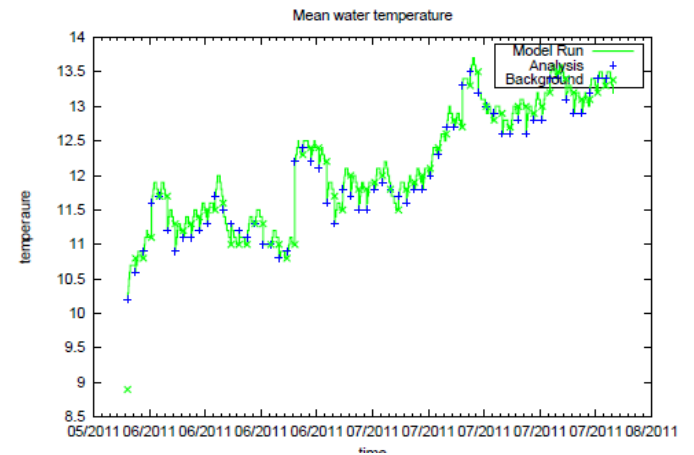
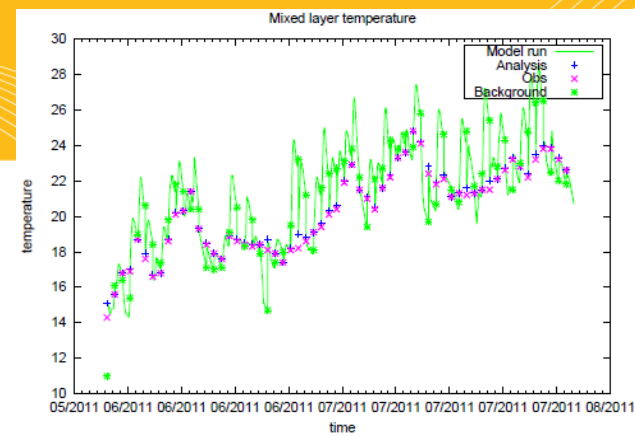
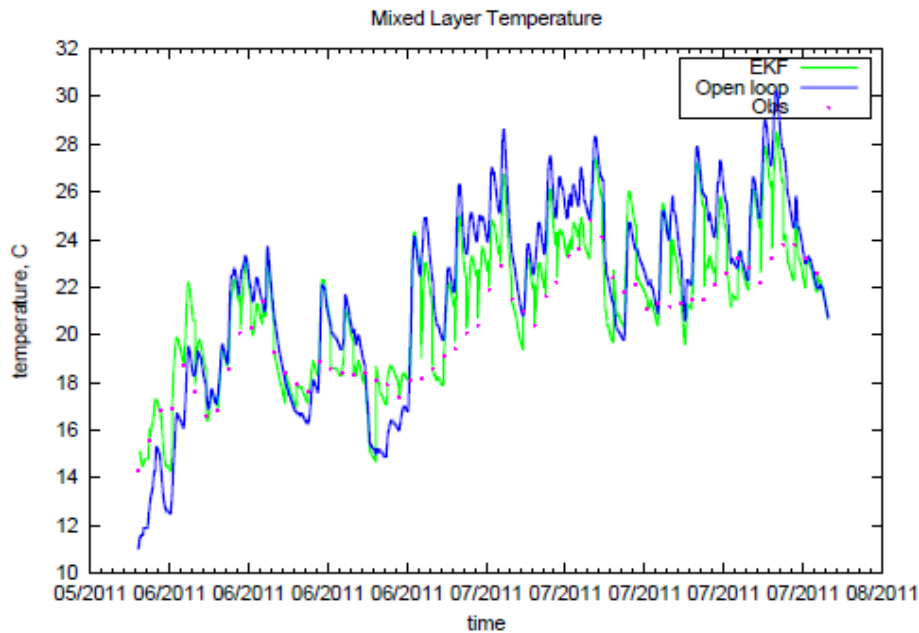
# Assimilation of SYKE obs

Lake Saimaa,

**BUT ...**

cold start at June, 1

... 2 months





## Plans, perspectives:

- Verification with independent obs or cross - validation
- Study errors
- Model bias corrections ... (mixed layer depth in stable regime) - if needed
- Testing with remote sensing obs
- OI with specific correlation functions
- Quality control for remote sensing obs
- Include into SURFEX/VARRASIM and HARMONIE

**Thank you for attention!**

