

**2nd Workshop on Parameterization of Lakes in  
Numerical Weather Prediction and Climate Modelling**  
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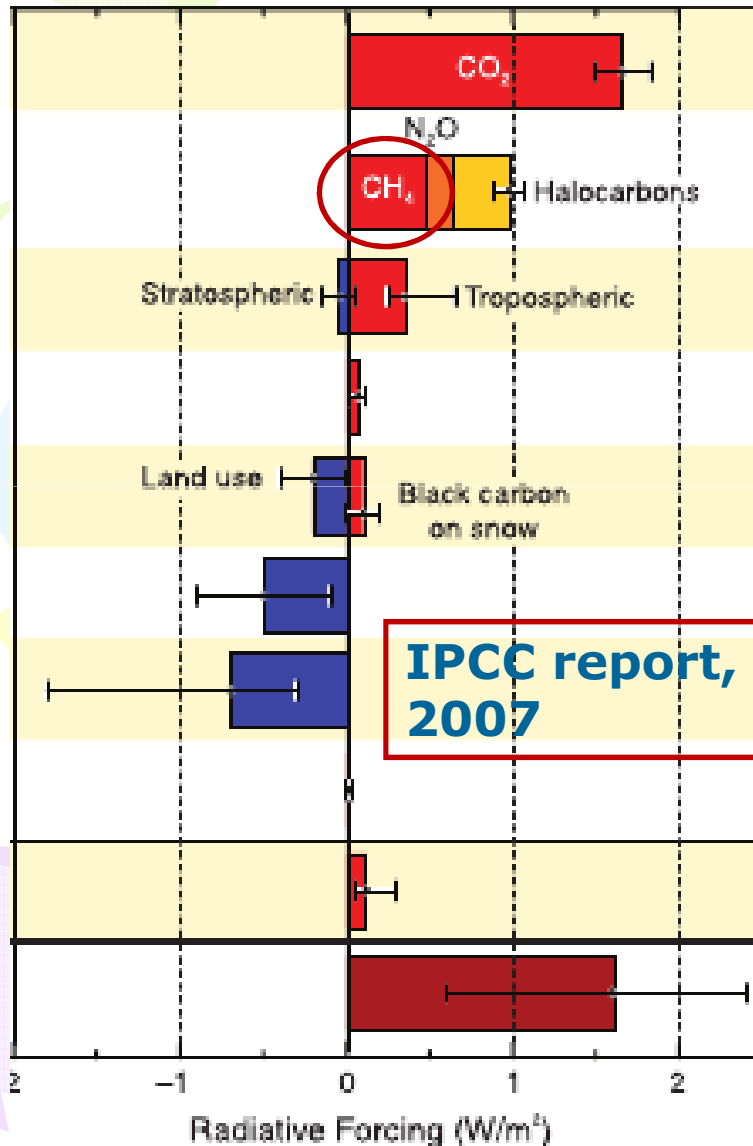
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# **Numerical modelling of methane emissions from thermokarst lakes**

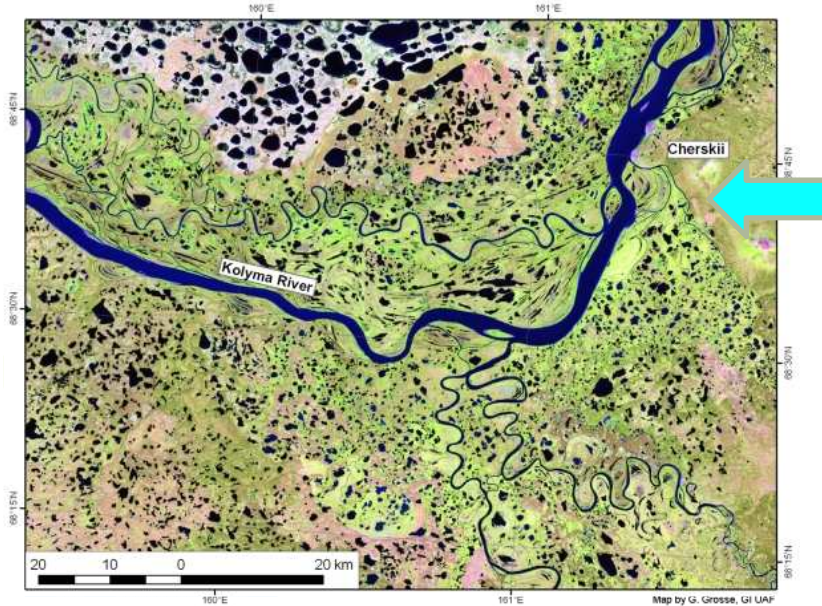
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# Atmospheric methane and its sources

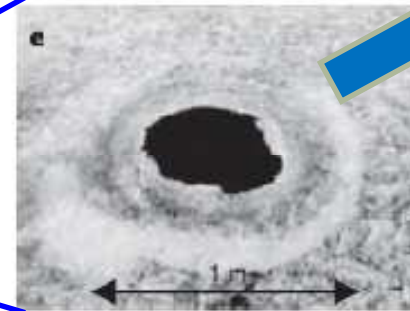
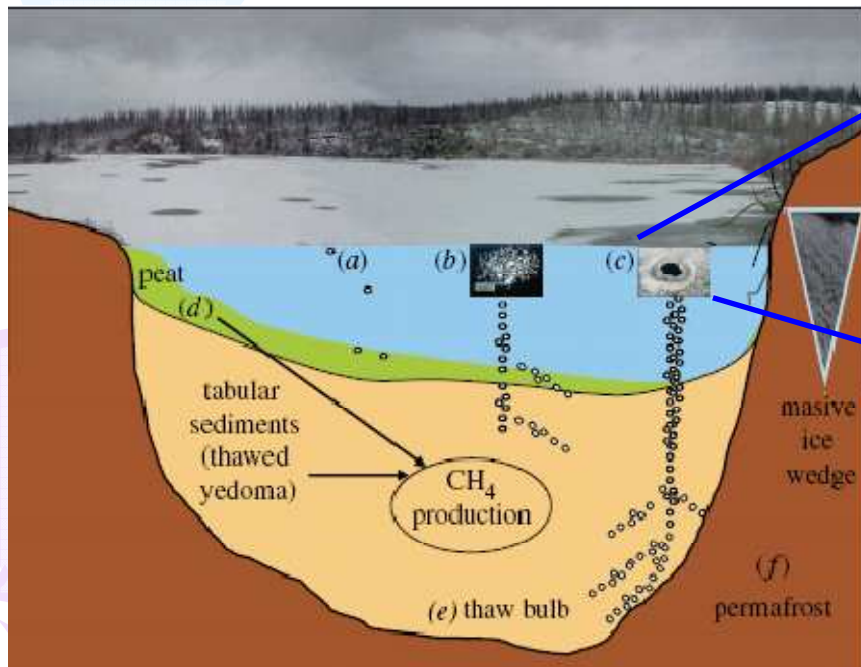


Sources of methane in a climate system	Mtonnes CH <sub>4</sub> /yr
Animals (mostly ruminants), without termites	106
Termites	23
Rice paddies	69
<b>Natural wetlands, excluding tundra</b>	<b>113</b>
<b>Tundra</b>	<b>19</b>
Oceans	14
<b>Lakes</b>	<b>5</b>
Methane hydrates	4
Volcanoes	1
Other natural sources	6
Burials of solid waste products	33
Coal industry	46
Gas industry	54
Biomass burning	40
Automobiles	1
<b>TOTAL</b>	<b>~530</b>

# Emission of methane by thermokarst lakes



- thermokarst lakes in Northern Siberia occupy 22-48% of the area
- satellite images indicate expanding of thermokarst lakes area

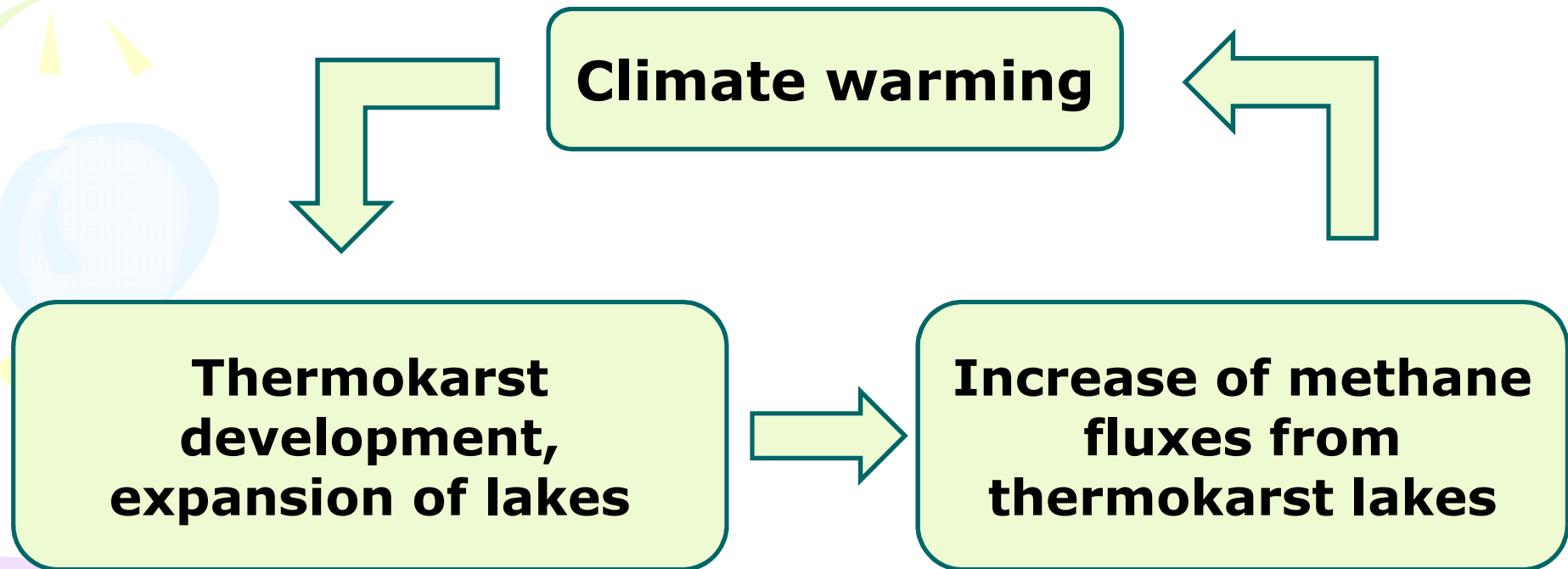


Unfreezing "hotspot" – the source of methane during wintertime

- 8 - 50% of anthropogenic emissions in XXI century depending on IPCC scenario (K. Walter et al., 2006, *Nature*)

# Implication to climate change and climate modeling

- Positive feedback:



**We need a modeling tool, a parameterization of thermokarst lakes' emissions in climate models**

# Methane emission: bogs and lakes

## Mechanism of methane production

- On **bogs** the substrate for methane production comes from surface NPP -> modeling approaches are well developed
- In **lakes** methane is produced (i) from lake bottom NPP and (ii) from the old organics, that has been sequestered in permafrost and comes to positive temperature region while talik is deepening -> the need for new parameterization

## Implication to annual cycle

- On **bogs** cold season emission is very low;
- In **lakes** methane is produced in talik, that is under positive temperatures all year round (40-50% of annual emission happen in cold period)

# Methane concentration in lake talik

$$\frac{\partial [CH_4]}{\partial t} = \frac{\partial}{\partial z} k_{CH_4, m} \frac{\partial [CH_4]}{\partial z} + P - E - \cancel{F}$$

(B. Walter & Heimann, 1996, 2000)

**Neglected:**

vegetation transport  $F$

**Ebullition:**

$$E = k_e f_{step} (\Delta[CH_4]) \Delta[CH_4],$$

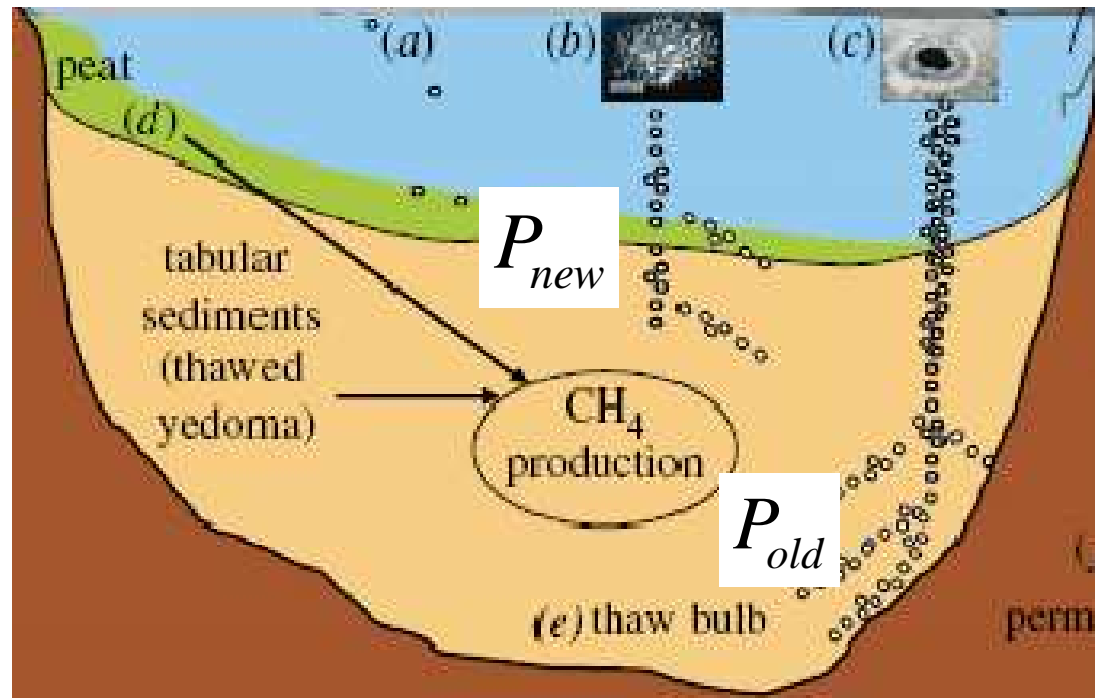
$$\Delta[CH_4] = [CH_4] - [CH_4]_{max}$$

**Production:**

$$P = P_{new} + P_{old}$$

$$P_{new} = P_{new,0} \exp(-\alpha_{new} z) f_{step}(T) q_{10}^{T/10}$$

$P_{new,0}$  - calibrated parameter



# Methane production from old organics decomposition

- happens only under positive temperatures
- is exponentially dependent on temperature
- is proportional to decomposable organics content

$$P_{old} = P_{old,0}^* C_{old} f_{step}(T) q_{100}^{T/10}$$

$P_{old,0}^*$  - calibrated parameter

**Michaelis-Menten equation for decomposition (1)**

$$\frac{\partial C_{old}}{\partial t} = -\frac{V_{C,max} C_{old}}{\alpha_C + C_{old}},$$

$$C_{old} = f(t, t_0, \alpha_C, V_{C,max})$$

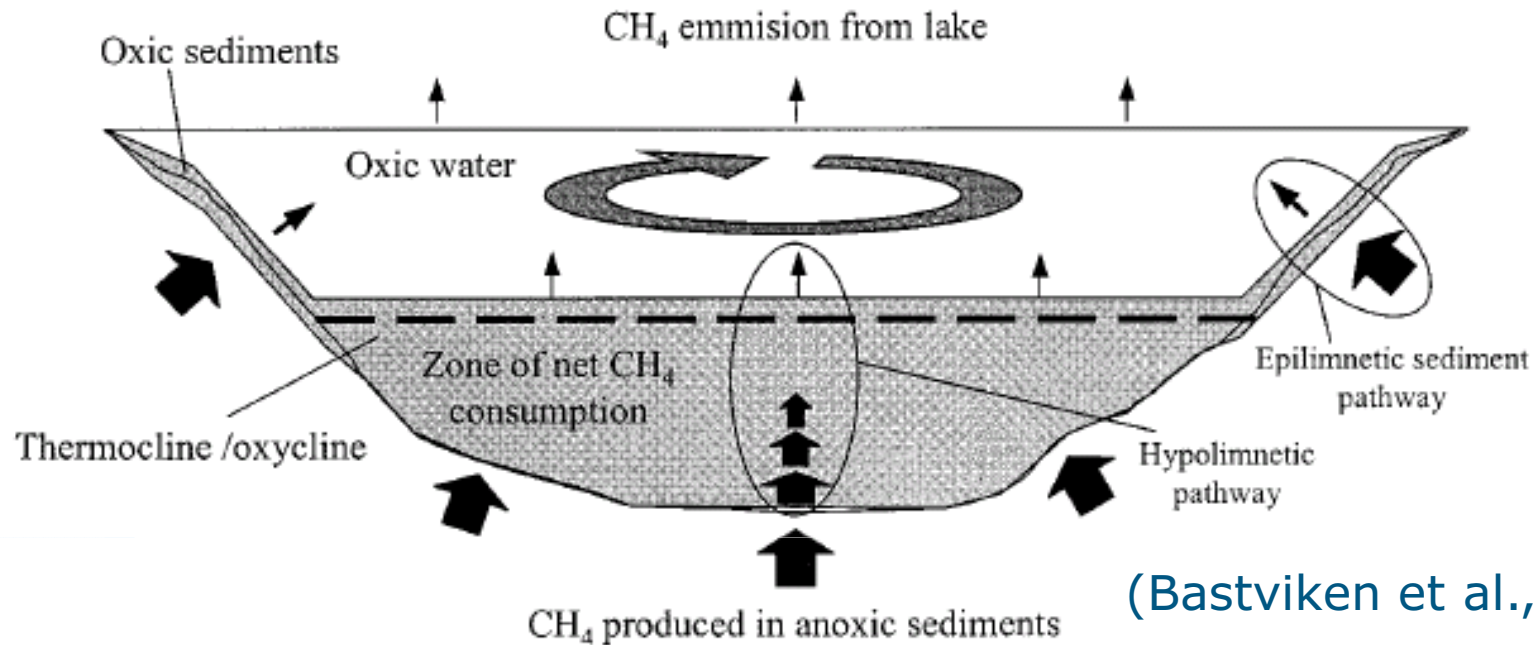
**Analytical law for talik deepening (2)**

$$z = C_t \sqrt{t_0}, \quad h_t = C_t \sqrt{t}$$

**Combining (1) and (2) yields**

$$C = C_{old,0} \left( 2 + \lambda_C - \sqrt{(1 + \lambda_C)^2 + 2\gamma_C C_t^{-2} (h_t^2 - z^2)} \right)$$

# Methane transfer in the water body



- **dissolved gases:**

- methane
- oxygen
- carbon dioxide

- **processes:**

- turbulent diffusion
- methane oxidation



$$\frac{\partial [\text{CH}_4]}{\partial t} = \frac{\partial}{\partial z} k_{\text{CH}_4} \frac{\partial [\text{CH}_4]}{\partial z} - V_{\text{oxid}},$$

$$\frac{\partial [\text{O}_2]}{\partial t} = \frac{\partial}{\partial z} k_{\text{O}_2} \frac{\partial [\text{O}_2]}{\partial z} - 2V_{\text{oxid}},$$

$$\frac{\partial [\text{CO}_2]}{\partial t} = \frac{\partial}{\partial z} k_{\text{CO}_2} \frac{\partial [\text{CO}_2]}{\partial z} + 2V_{\text{oxid}}$$



# One-dimensional k-ε model (LAKE)

## Heat equation

$$\frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left( k_T \frac{\partial T}{\partial z} \right) - \frac{1}{c_p \rho} \frac{\partial S}{\partial z} + \frac{1}{A} \int_{\Gamma_A} (\vec{u} \cdot \vec{n}) T dl$$

## Momentum equations

$$\frac{\partial u}{\partial t} = \frac{\partial}{\partial z} k_M \frac{\partial u}{\partial z} + fv - g \cdot \text{tg} \alpha_x - C_{veg} u \sqrt{u^2 + v^2},$$

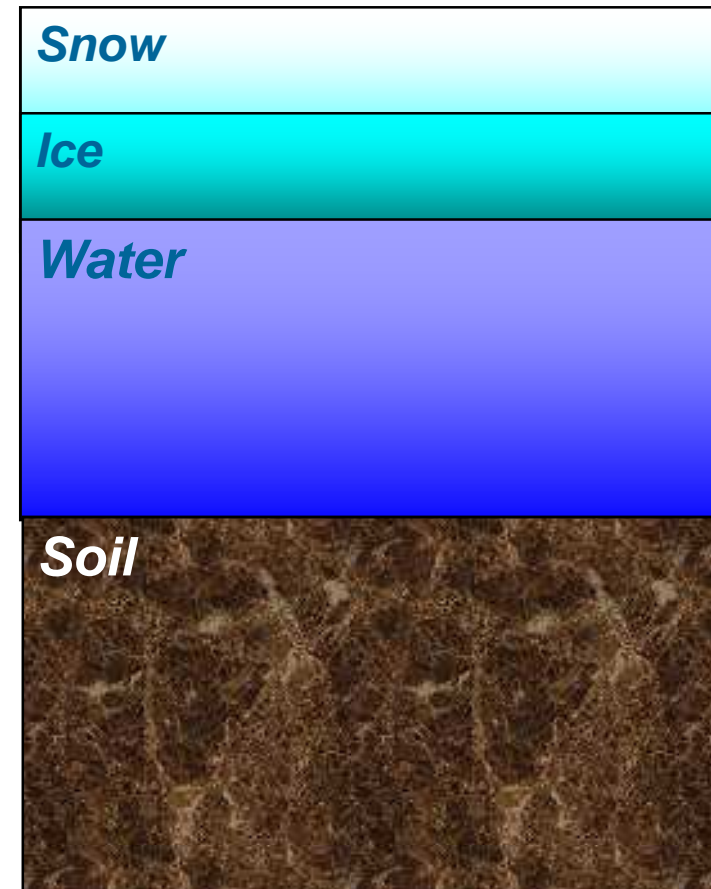
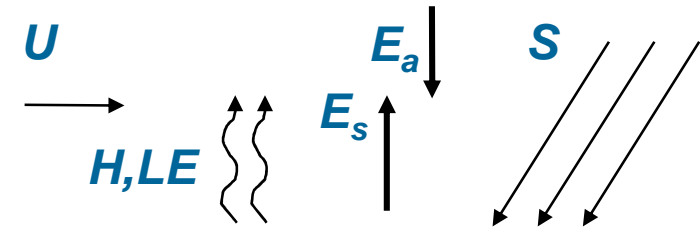
$$\frac{\partial v}{\partial t} = \frac{\partial}{\partial z} k_M \frac{\partial v}{\partial z} - fu - g \cdot \text{tg} \alpha_y - C_{veg} v \sqrt{u^2 + v^2}$$

## K-ε turbulence closure

$$k_M = C_e \frac{E^2}{\varepsilon},$$

$$\frac{\partial E}{\partial t} = \frac{\partial}{\partial z} \left( \nu + \frac{k_M}{\sigma_E} \right) \frac{\partial E}{\partial z} + P + B - \varepsilon,$$

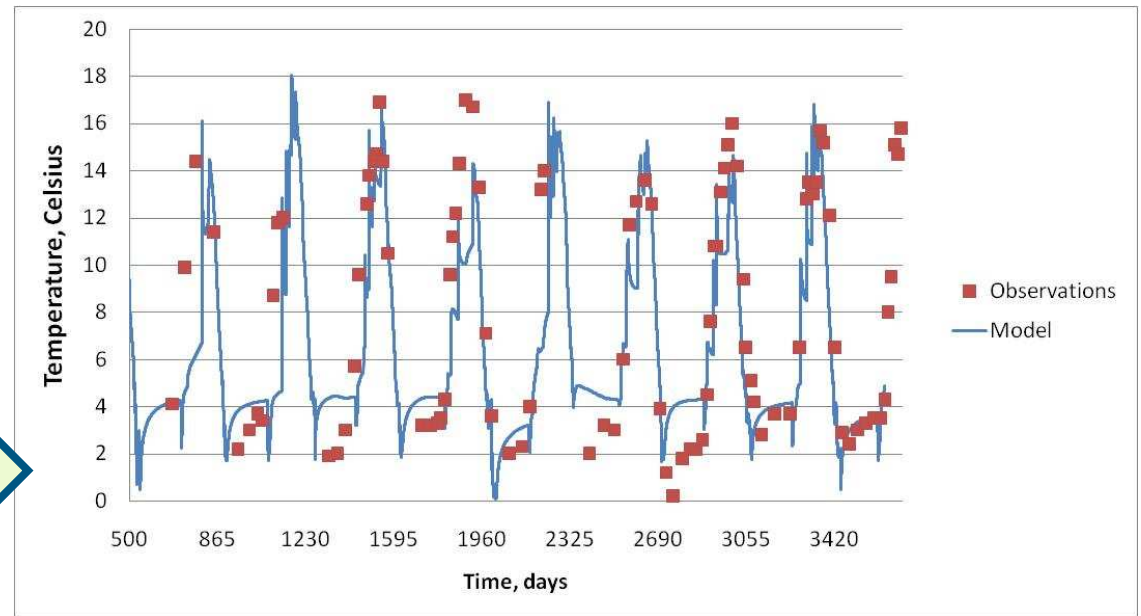
$$\frac{\partial \varepsilon}{\partial t} = \frac{\partial}{\partial z} \left( \nu + \frac{k_M}{\sigma_\varepsilon} \right) \frac{\partial \varepsilon}{\partial z} + \frac{\varepsilon}{E} (c_{1\varepsilon} P + c_{3\varepsilon} B - c_{2\varepsilon} \varepsilon)$$



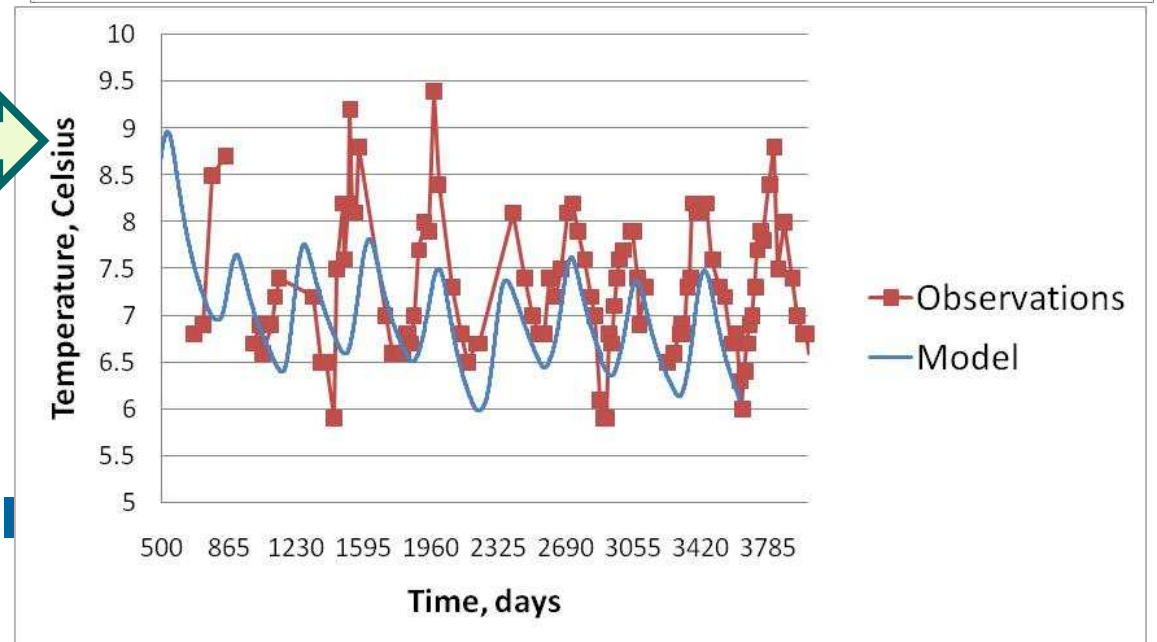
# Validation: sediments temperature

- Krasnoe Lake, (near S.-Petersburg)
- 1969 – 1979
- Sortavala station forcing

Bottom temperature



Bottom sediments temperature (3 m depth)

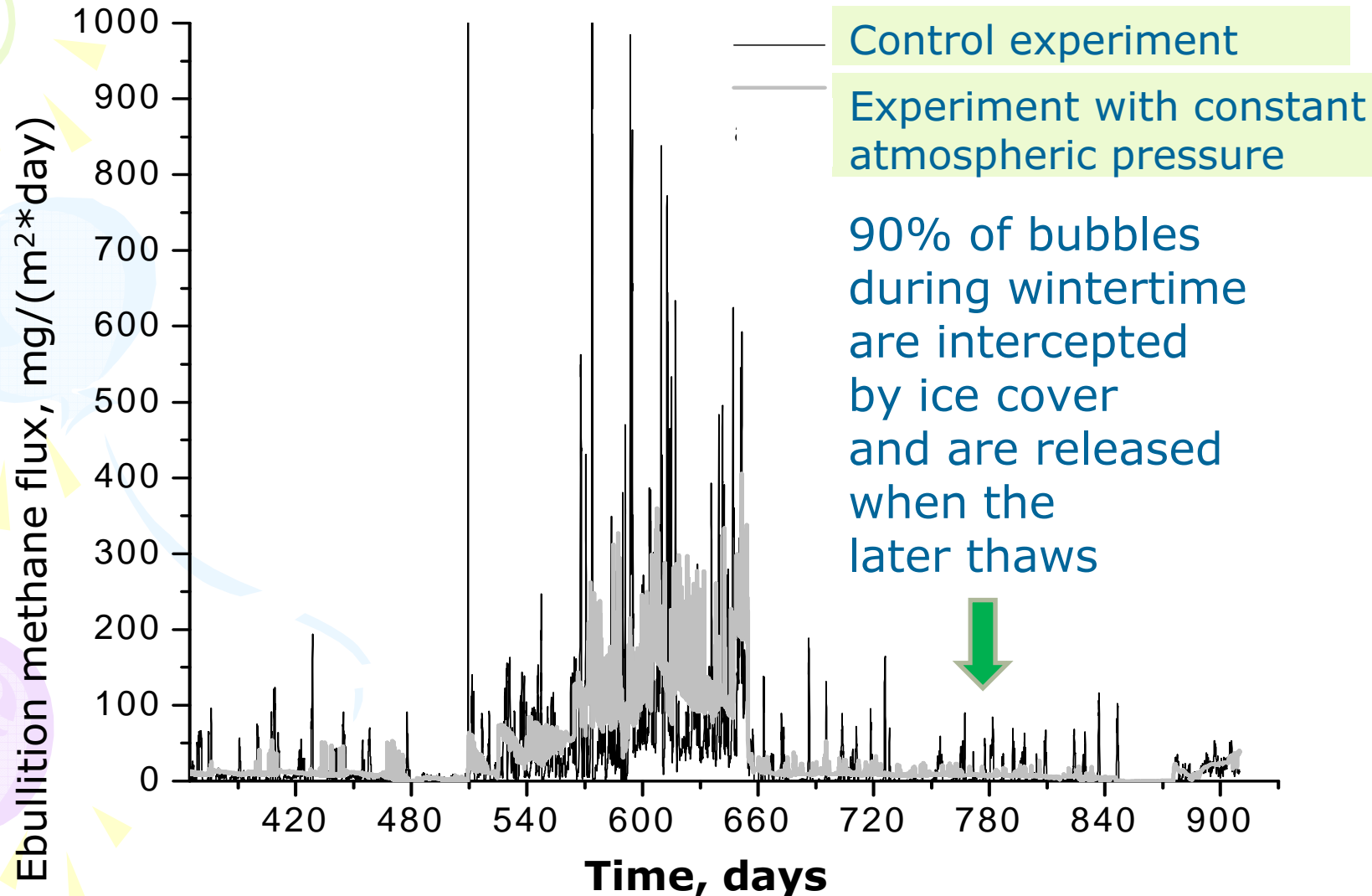


Observations:  
Kusmenko, 1976.

Soil heat conductance:  
Cote and Konrad model  
(Sen Lu et al., 2007)

# Case study: Lake Shuchi

- Time series of atmospheric variables as input to lake model are extracted from ERA-Interim reanalysis



# Model calibration: Lake Shuchi

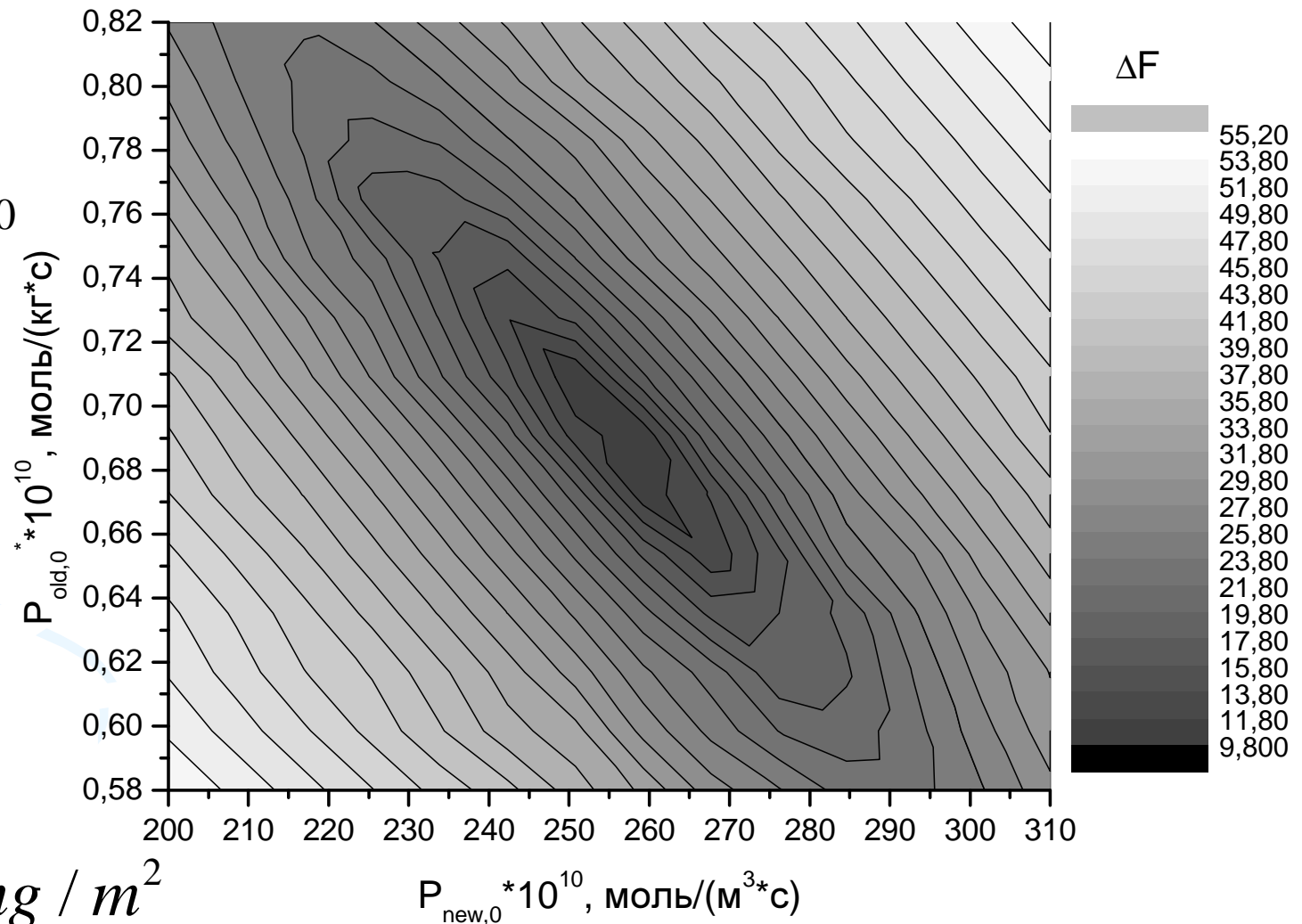
The measure of model error

$$\Delta F^2 \equiv \left( F_a^w - F_{a,m}^w \right)^2 + \left( F_a^s - F_{a,m}^s \right)^2$$

- Calibrated parameters

$$P_{old,0}^*, P_{new,0}$$

- $\Delta F$  has single minimum



$$\Delta F_{min} \cong 10 \text{ mg} / \text{m}^2$$

$$P_{new,0} \cdot 10^{10}, \text{ моль}/(\text{м}^3 \cdot \text{с})$$

# Model validation


**Observations: Lake Shuchi** (K. Walter et al., 2006)  
 hourly observations of ebullition and diffusion methane fluxes in different lake sections for 2003 – 2004

	Annual methane emission, mg/(m <sup>2</sup> *yr)	A part of open-water period emission, %	A part of ice-covered period emission, %
<b>Observations</b>	<b>22658</b>	<b>54</b>	<b>46</b>
<b>Model</b>	<b>22588</b>	<b>54</b>	<b>46</b>

	Open water period	Ice-covered period
A part of young methane in emissions (observations), %	<b>47</b>	<b>6</b>
A part of young methane in net generation (model), %	<b>61</b>	<b>32</b>





## Remarks on lake methane model

- The values of calibrated parameters depend on errors (lack of observations!) of input parameters: lake depth, water turbidity, atmospheric forcing, etc.
  - The model should be verified on a significant number of thermokarst lakes
  - The model still does not consider thermokarst lake development (deepening, drainage, etc.)
- 



# Perspectives

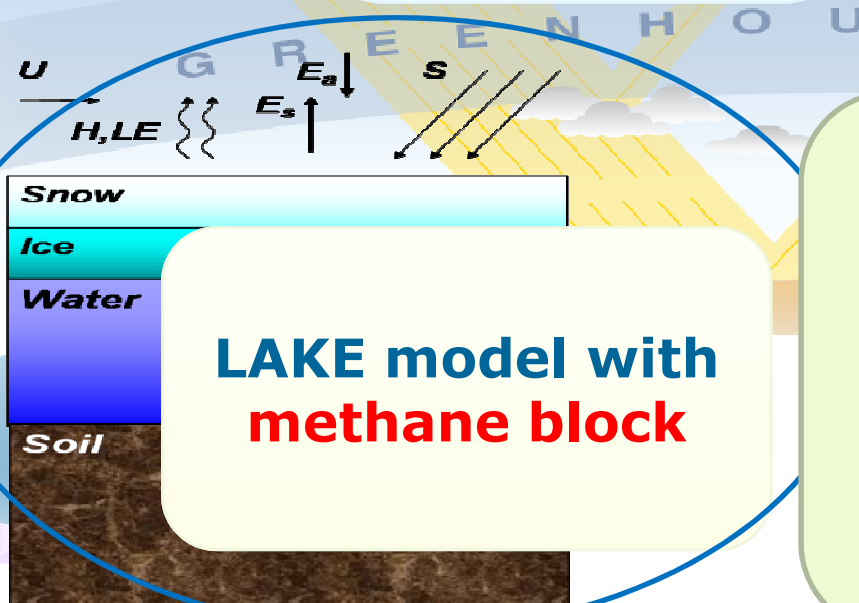
- Estimation of atmospheric methane balance at a regional scale using reanalysis and/or regional atmospheric modeling with satellite retrieval of atmospheric methane to assess intensity of surface sources
  - Incorporation of lake methane model in regional and global climate models to assess regional feedback between climate change and thermokarst lakes and its global significance
- 
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# Regional atmospheric model NH3D\_MPI

Atmospheric  
3D dynamics in  
 $\sigma$ -coordinates,  
**methane  
transport and  
chemistry**

Land surface model of  
**INM:**

1. Soil (including permafrost)
2. Vegetation
3. Snow cover
4. **Walter and Heimann methane model for bogs**
5. **A set of models for oxic soils carbon cycling**



**LAKE model with  
methane block**

- horizontal spacing 1-10 km
  - >30 levels in vertical
- **parallel implementation using MPI**