



# **Numerical simulation of high-frequency normal atmospheric modes in the non-isothermal atmosphere with + Newtonian cooling**

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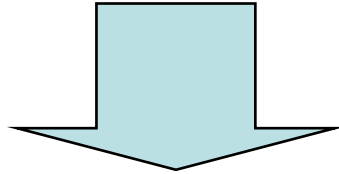
# Content:

- ❑ Linearized theory of global-scale atmospheric waves:
  - **basic equations;**
  - **the vertical structure equation.**
- ❑ Simulation results (numerical solution of the vertical structure problem):
  - **Amplitude distribution (the atmospheric resonance);**
  - **Phase profile;**
  - **The vertical profile of energy flux.**

# N=1 Kelvin normal mode:

Period – about 33-hours

Horizontal phase speed – close to the speed of sound

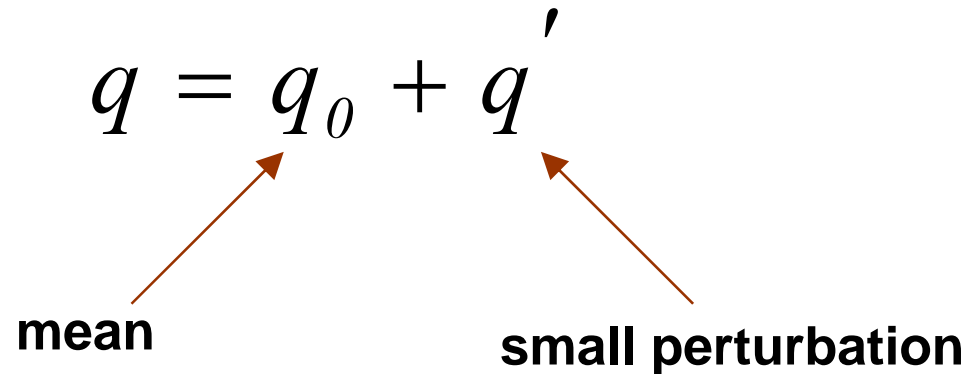


Largely unaffected by mean wind

# Linearized wave theory:

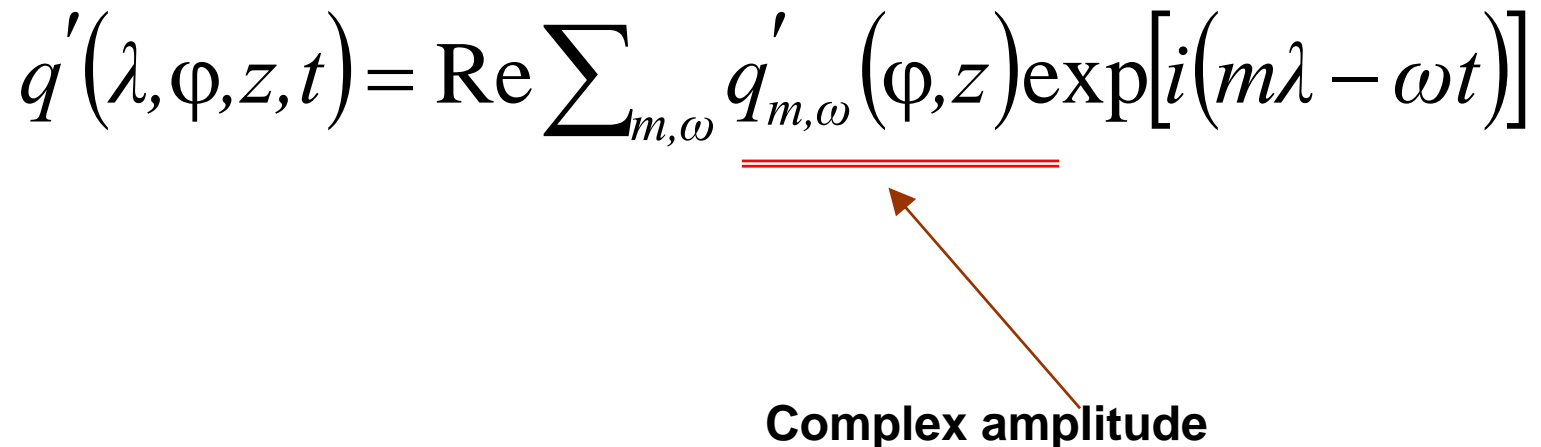
$$q = q_0 + q'$$

mean small perturbation

The diagram shows the equation  $q = q_0 + q'$ . Below  $q_0$  is the word "mean" with an orange arrow pointing to  $q_0$ . Below  $q'$  is the phrase "small perturbation" with an orange arrow pointing to  $q'$ .

$$q'(\lambda, \varphi, z, t) = \text{Re} \sum_{m, \omega} \underline{q'_{m, \omega}(\varphi, z)} \exp[i(m\lambda - \omega t)]$$

Complex amplitude

The diagram shows the equation  $q'(\lambda, \varphi, z, t) = \text{Re} \sum_{m, \omega} \underline{q'_{m, \omega}(\varphi, z)} \exp[i(m\lambda - \omega t)]$ . The term  $q'_{m, \omega}(\varphi, z)$  is underlined in red. Below the underline is the text "Complex amplitude" with an orange arrow pointing to the underlined term.

Basic equations for complex amplitudes  
(without subscripts  $m, \omega$ ):

$$-i\omega u' - f v' = -i m p' / (\rho_0 a \cos \varphi),$$

$$-i\omega v' + f u' = -p'_\varphi / (\rho_0 a),$$

$$p'_z = -\rho' g,$$

$$-i\omega \rho' / \rho_0 + i m u' / (a \cos \varphi) + (\cos \varphi v')_\varphi / (a \cos \varphi) + (\rho_0 w')_z / \rho_0 = 0,$$

$$-i\omega p' + (p_0)_z w' = c_s^2 (-i\omega \rho' + (p_0)_z w') + (\gamma - 1) \rho_0 (J' - \underline{a_N T'}),$$

$$\frac{p'}{p_0} = \frac{\rho'}{\rho_0} + \frac{T'}{T_0}.$$

Heating

Newtonian cooling

# Separation

$$\phi' = \sum_n \Theta_n(\varphi) G_n(z)$$
$$F' = \sum_n \Theta_n(\varphi) F_n(z)$$

Hough function  $\Theta_n$  transform

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$$L_\varphi[\phi'] = L_z[\phi'] - F'$$

Latitudinal structure equation  
(Laplace's tidal equation)

Vertical structure equation

$h_n$

Separation parameter  
(equivalent depth)

## Vertical structure equation (log-isobaric coordinates)

$$\frac{d^2 G_n}{d x^2} + M \left[ N^2; a_N \right] \frac{d G_n}{d x} + \frac{H^2 N^2}{g h_n} G_n = F_n'$$

$$x = -\ln(P/P_0)$$

$$H = \frac{R \bar{T}}{g}$$

$$N^2 = \frac{R}{H} \left( \frac{dT_0}{dx} + \kappa \frac{T_0}{H} \right)$$

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### Boundary conditions:

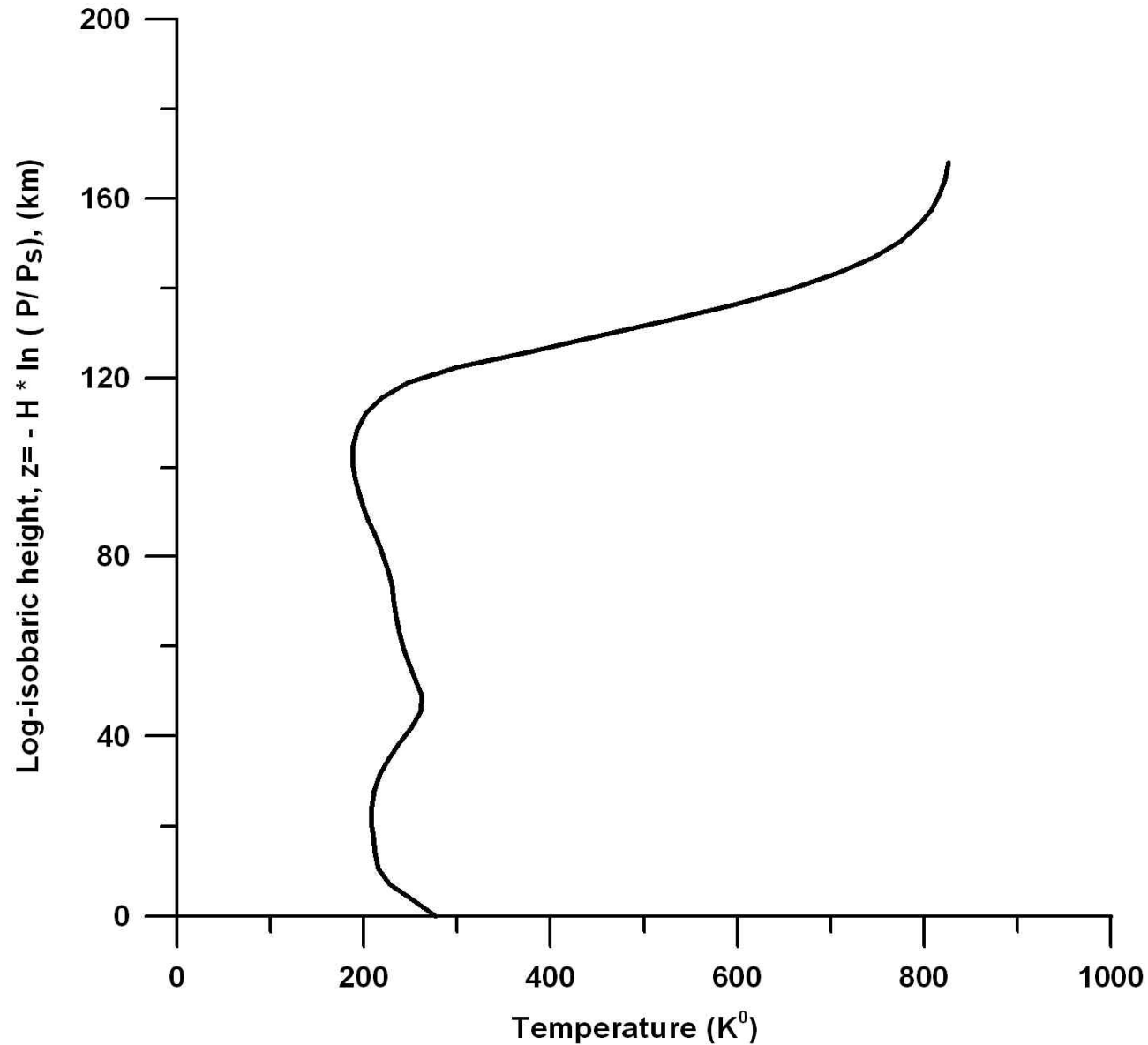
Upper -

Radiation\finite  
energy condition

Lover -

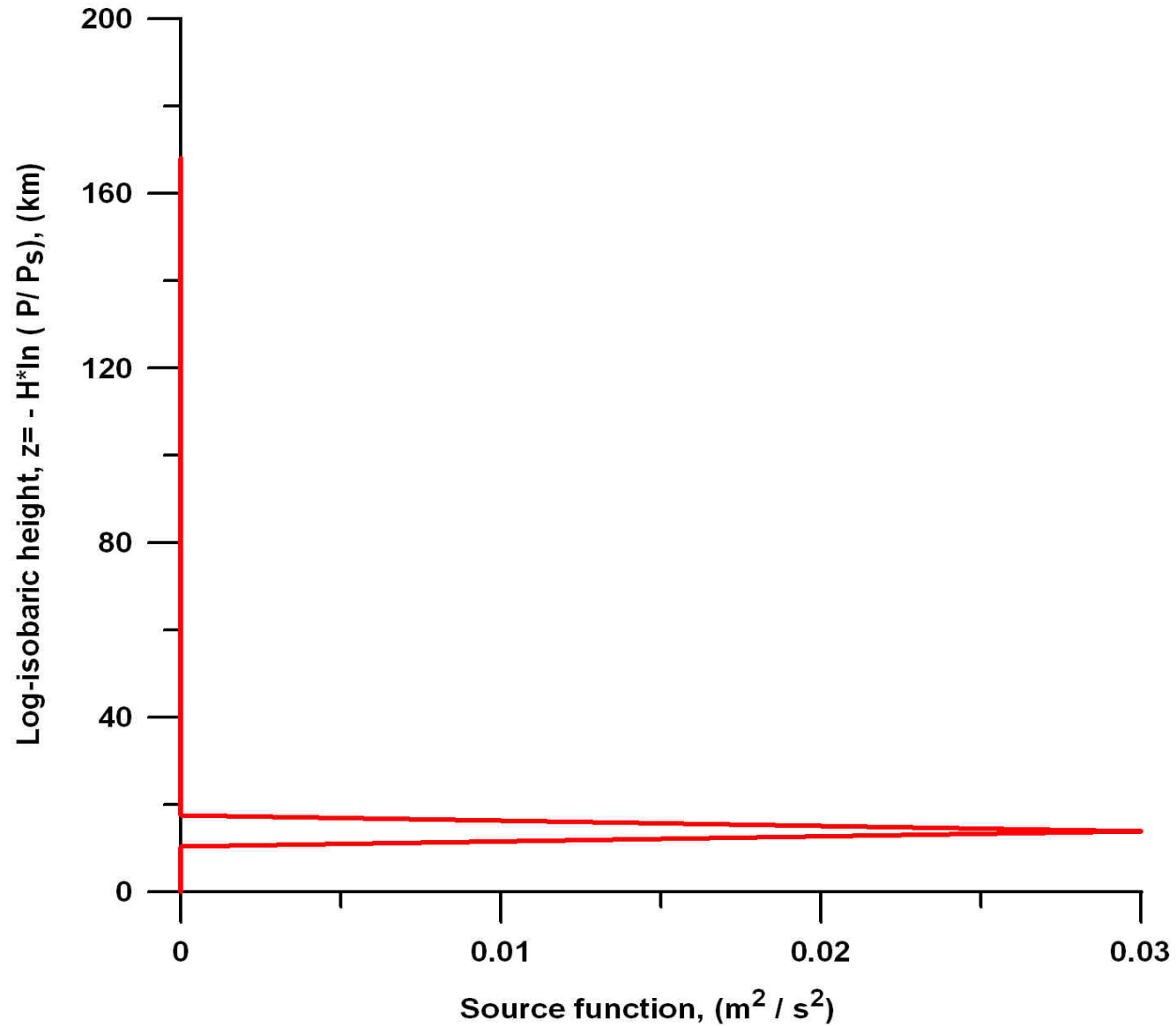
No vertical velocity  
disturbance  
condition

# Mean distribution of temperature used in calculation

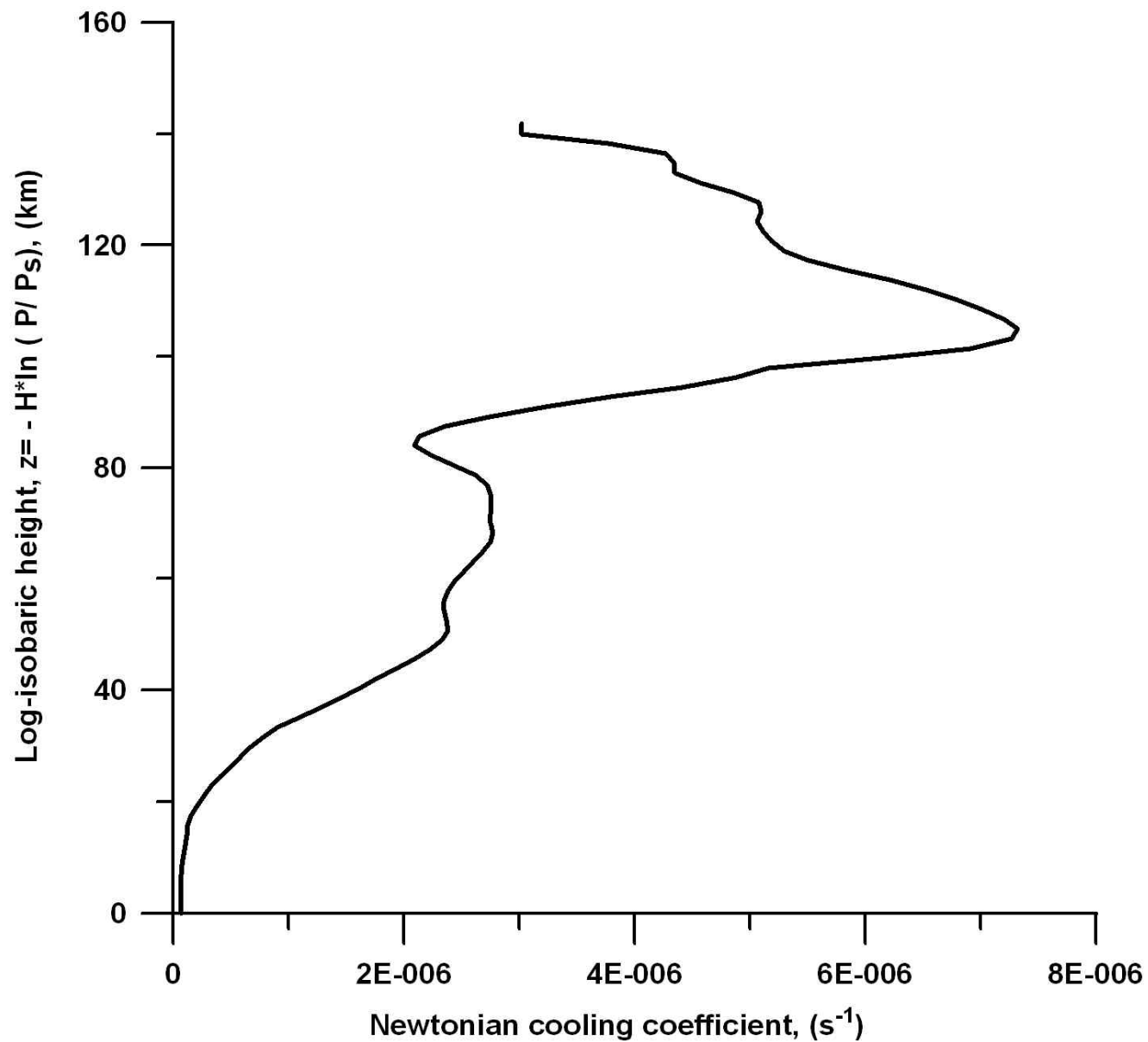




# Source function:

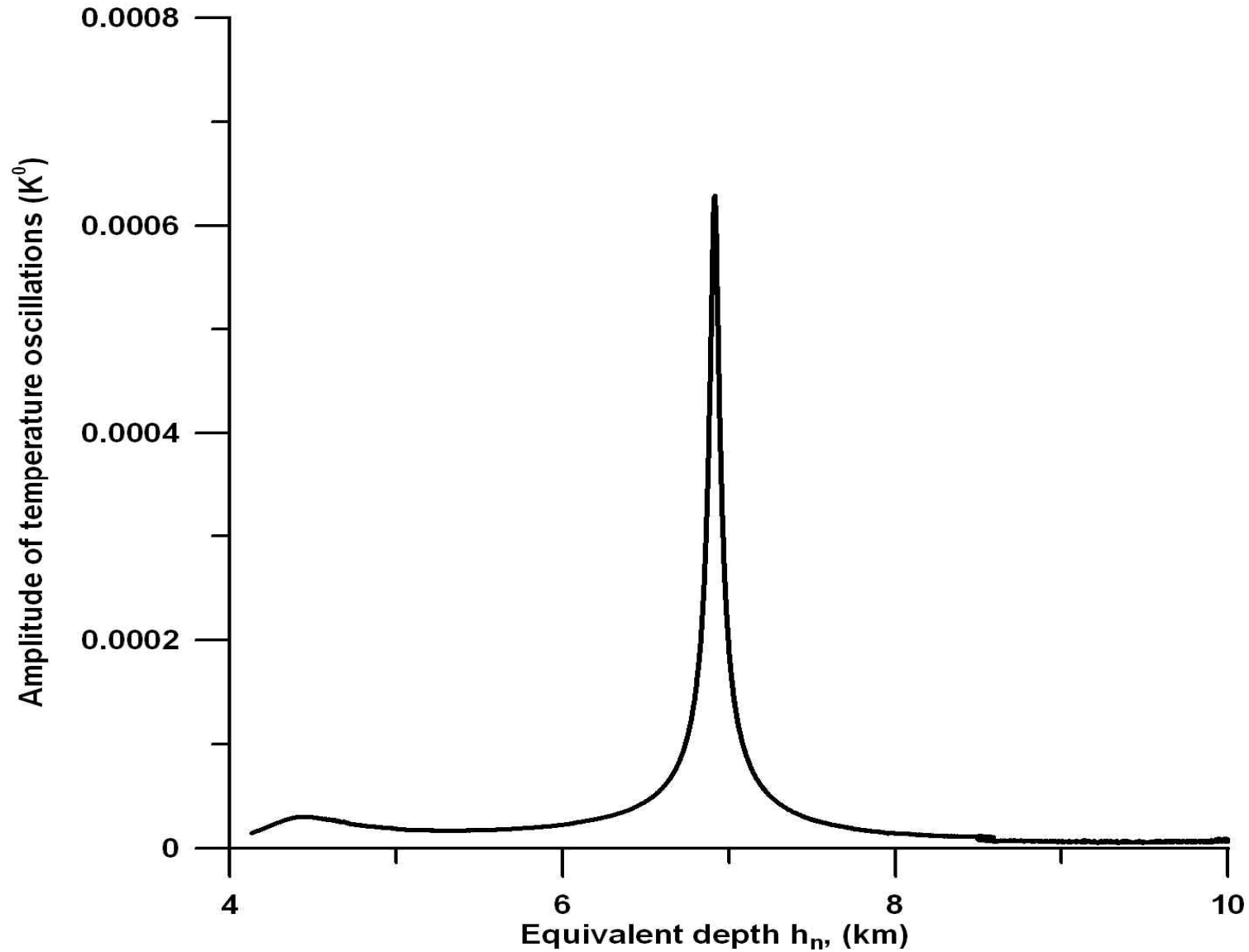


# Newtonian cooling coefficient ( $a_N$ )

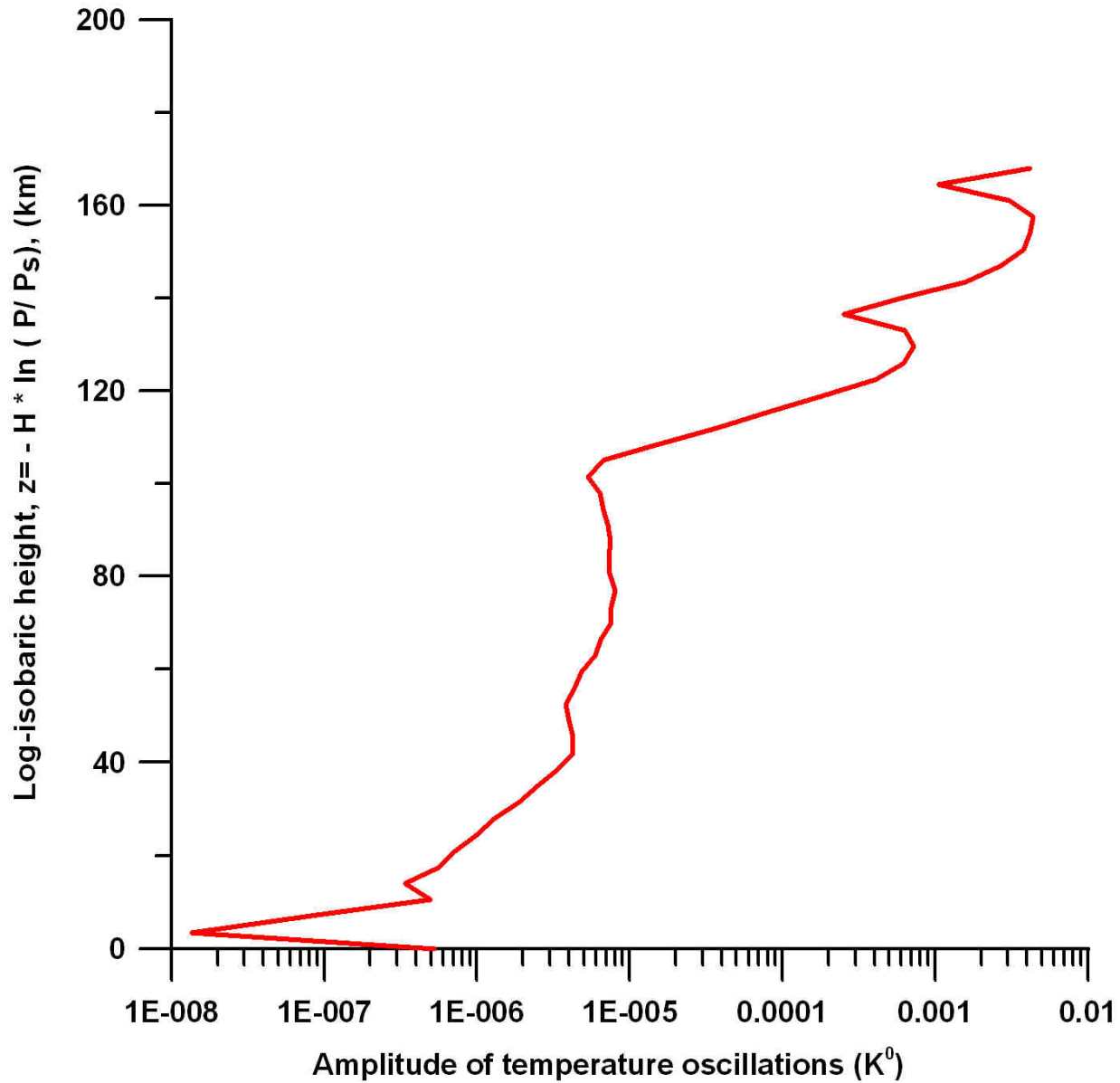


# Simulation results

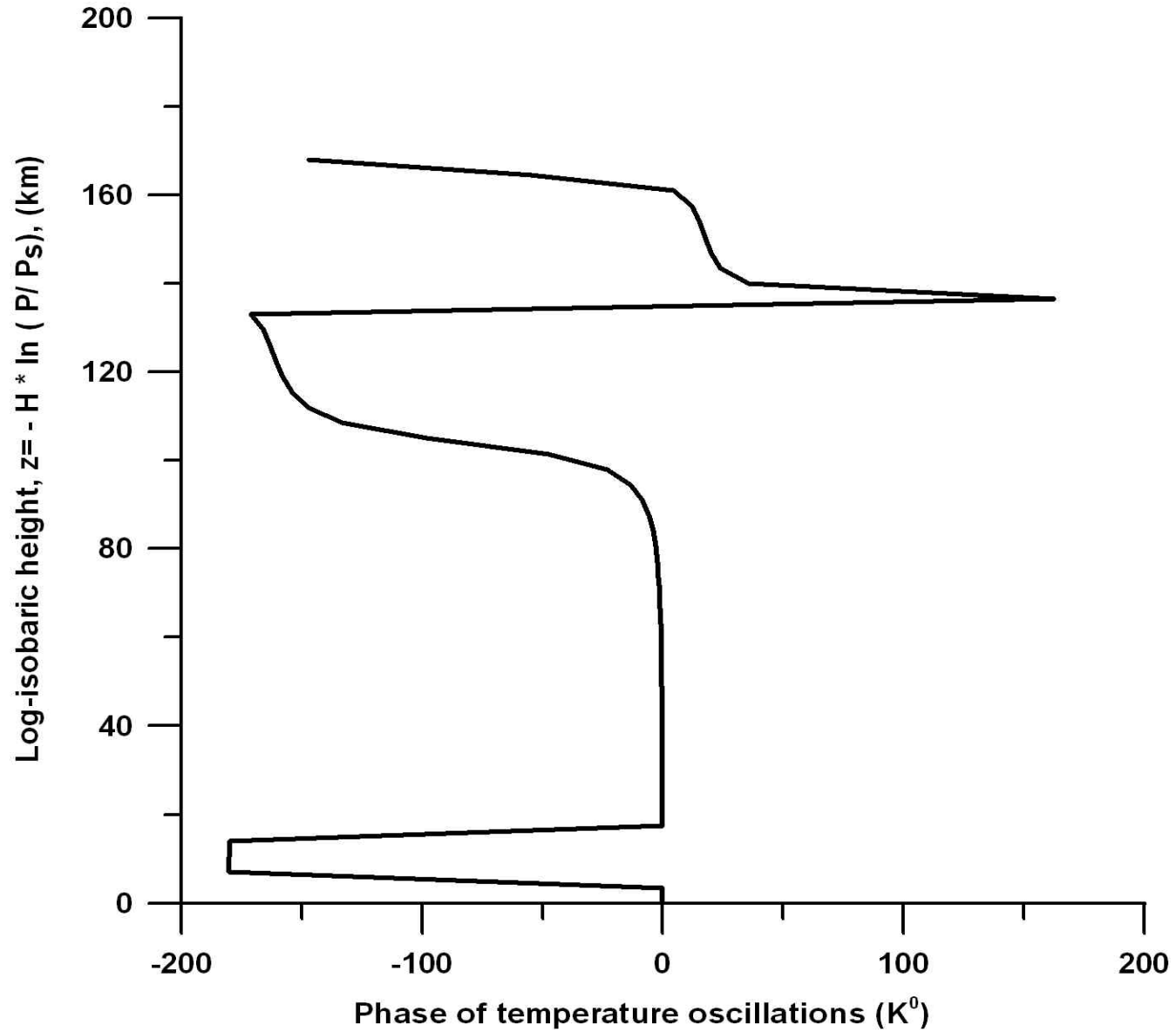
Atmospheric response (LI-height  $z=80\text{km}$ )



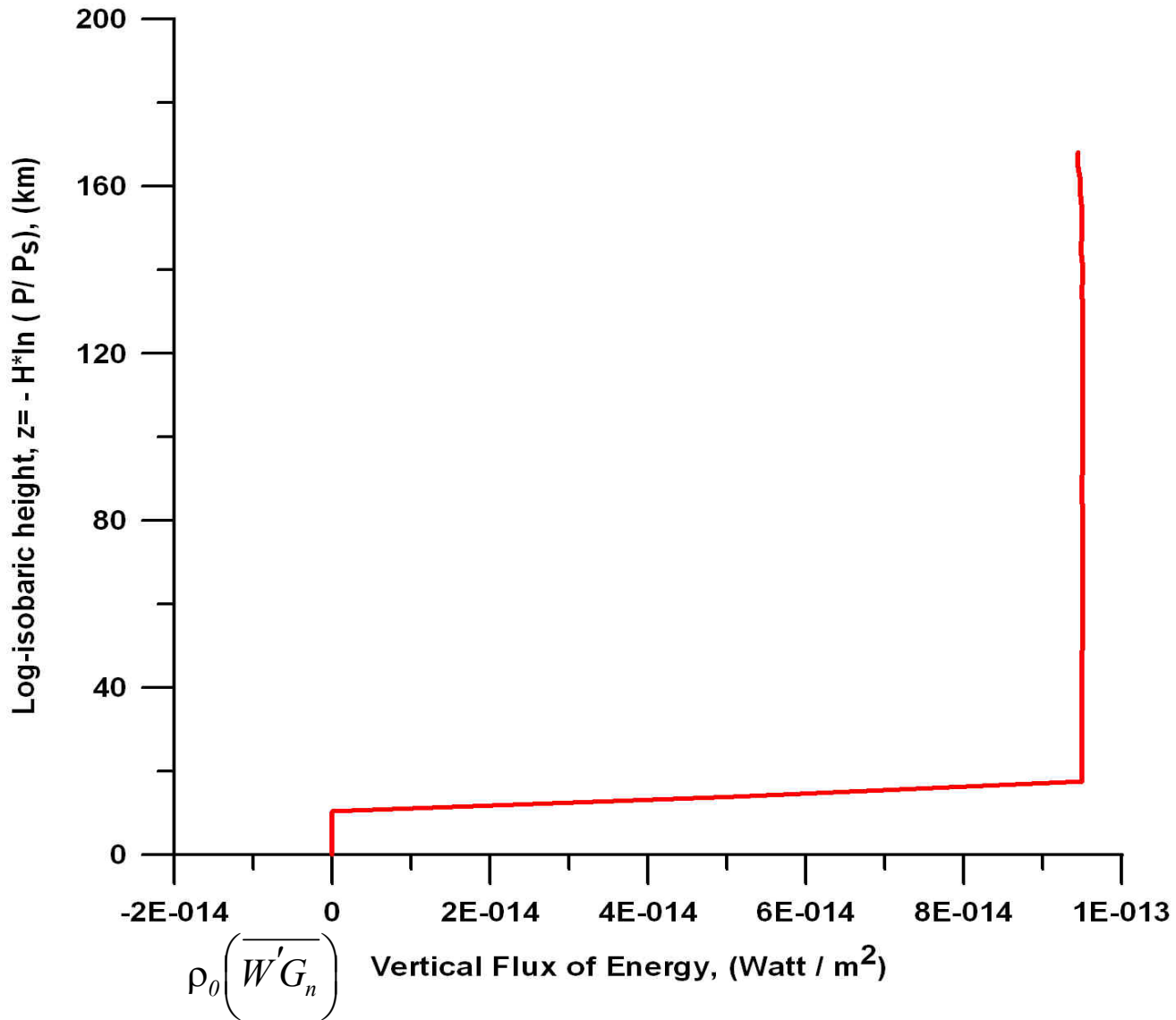
# Amplitude as a function of height (NM)



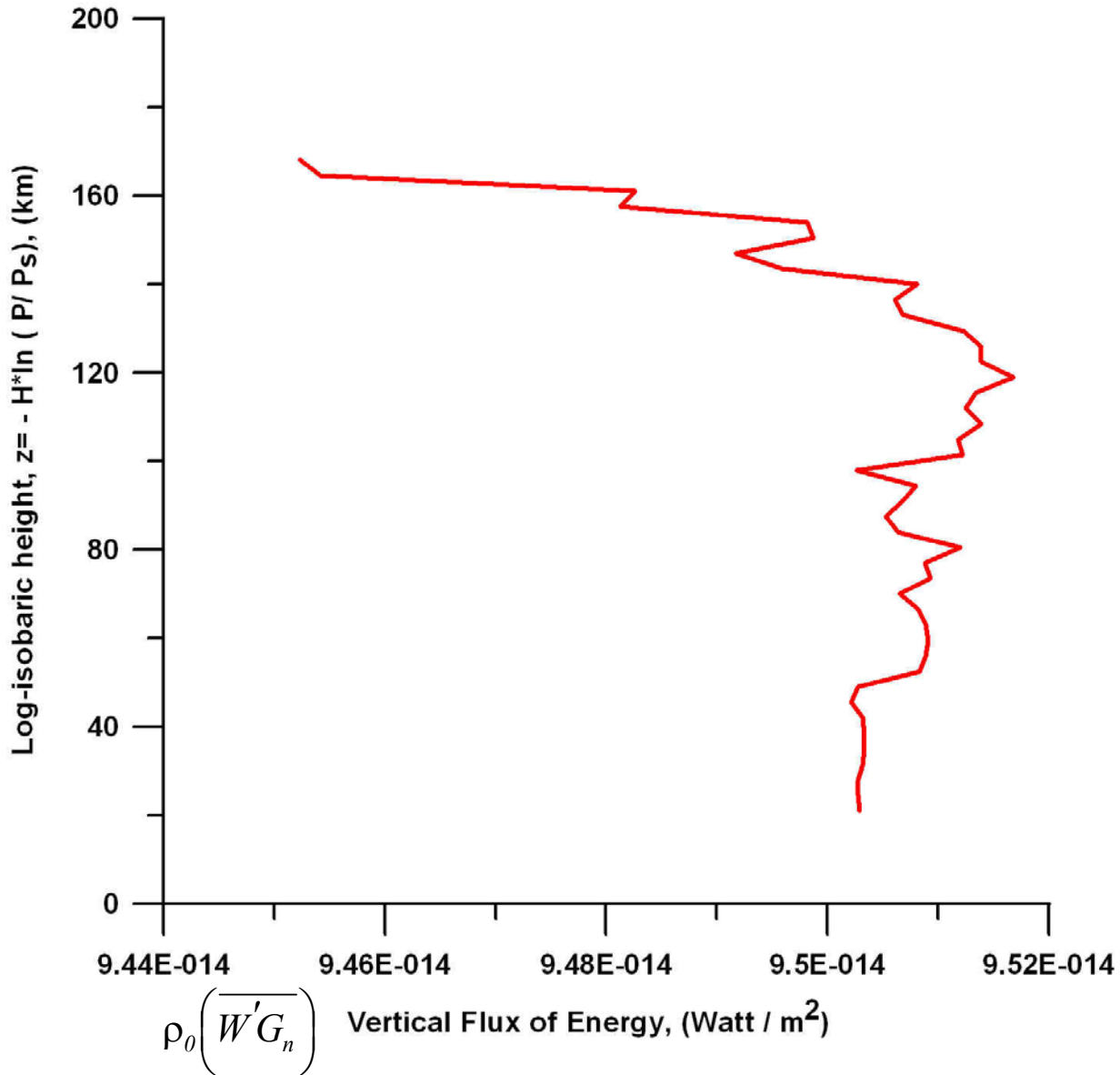
# Phase as a function of height (NM)



# Vertical flux of energy



# Vertical flux of energy (upper part of previous figure)





**Thank You!**





**CAUSES**

**Climate and Weather of the  
Sun-Earth System**

The New SCOSTEP Program for  
2004-2008

# Sea level pressure spectrum

(obtained by K. Hamilton and R. Garcia)

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