

# Use of ground-based GNSS measurements in data assimilation

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GNSS\* positioning

Tropospheric delay

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Zenith Delays

Slant Delays

\*) <u>G</u>lobal <u>Navigation Satellite</u> System



### **Introduction**

**Global Navigation Satellite Systems** 

The most accurate positioning applications utilize navigation satellite systems

- GPS (<u>G</u>lobal <u>Positioning System</u>)
- GLONASS (<u>Glo</u>balnaja <u>Na</u>vigatsionnaja <u>S</u>putnikovaja <u>S</u>istema)
- Galileo



GPS Nominal Constellation 24 Satellites in 6 Orbital Planes 4 Satellites in each Plane 20,200 km Altitudes, 55 Degree Inclination





GNSS positioning



Navigation satellites broadcast signals modulated on two microwave frequencies

Travel times of the electromagnetic signals are interpreted as distance measurements

The distance measurements are utilized by linear algebra to determine the receiver coordinates





### **Introduction**

#### GNSS observation equation

GNSS positioning is based on solving the unknown parameters of observation equation

$$\Phi = \frac{1}{\lambda}\varrho + \frac{c}{\lambda}(\delta_R - \delta^S) + N_i + \Delta^T + \Delta^I$$

 $\delta^{S}$ 

 $\Delta^{\prime}$ 

Φcarrier phase $\lambda$ wavelength $\varrho$ distance

c speed of light

- $\delta_{\mathsf{R}}$  receiver clock error
  - satellite clock error
- *N<sub>i</sub>* integer ambiguity
- $\Delta^{T}$  <u>tropospheric refraction</u>
  - ionospheric refraction

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### **Introduction**

#### Tropospheric delay

The tropospheric delay  $\Delta^T$  is a consequence of the decrease of the microwave propagation speed in the neutral atmosphere

$$\Delta^T = \int\limits_s (n-1)ds = 10^{-6} \int\limits_s Nds$$

The tropospheric delay

- appears as increase in the measured distance
- can be estimated as a by-product of geodetic processing
- is an integral of refractivity *N* along the signal path *s* through the atmosphere
- can be considered as an observation of atmospheric humidity





Properties of tropospheric delay

In case the signal comes from zenith, the tropospheric delay induces an apparent increase of ca. 2.5 m in distance measurement

Tropospheric delay is dominated by the hydrostatic component, which is accurately modelled using surface pressure only

The remaining part:

- is called *wet delay*
- is difficult to parameterize in terms of surface meteorology
- is responsible for most of the noise in geodetic applications
- is *closely related with atmospheric humidity* and therefore is of interest in meteorology



General aspects

Advantages

- dense observing networks can be built and maintained with low cost
- temporal resolution of measurements is good
- quality of observations is independent of weather

Disadvantages

- observations are subject to heavy preprocessing
- observation error statistics are complicated
- vertical resolution is poor



Observations

In their raw format, the observations consist of a group of *pseudorange measurements* between the transmitting GNSS satellite and the receiver

Geodetic processing allows production of meteorological observations:

- Zenith Delays
  - Integrated Water Vapour
- Slant Delays



Zenith Delays

Zenith Total Delay (ZTD) represents tropospheric delay in a vertical column

- Zenith Hydrostatic Delay (ZHD) represents surface pressure
- Zenith Wet Delay (ZWD) represents the amount of water vapour in the vertical column





Integrated Water Vapour

Using atmospheric temperature and humidity profiles, ZWD can be converted to Integrated Water Vapour (IWV)

$$IWV = \left[10^{-6} \left(\frac{k_3}{T_m} + k_2'\right) \rho_v R_v\right]^{-1} ZWD$$

This can be useful for comparison purposes (e.g. against radiosonde measurements or satellite retrievals)

However, the conversion *increases noise level* and *complicates the observation error statistics* 

➔ use of IWV is not recommended in data assimilation



Slant Delays

Slant Total Delay (STD) represents tropospheric delay along the actual signal path through the atmosphere

STD can be separated in hydrostatic and wet components and processed further to Slant Water Vapour (SWV)





Observations from NWP point of view

#### Zenith Delay

- Processing and assimilation architectures close to operational
- Isotropic atmosphere assumed – may be suboptimal near fronts
- Shows potential for nowcasting, synoptic scale data assimilation and climate monitoring

#### **Slant Delay**

- Processing and assimilation methods are still *under development*
- Captures anisotropic structures in fine scales, e.g. humidity gradients
- Shows potential for *fine scale data* assimilation and tomography



### Observation modelling

#### Tropospheric Delay

Observation operators for tropospheric delays integrate the model refractivity as determined by pressure, temperature and humidity fields

$$\Delta^{T} = \int_{s} (n-1)ds = 10^{-6} \int_{s} Nds$$
$$N = k_{1} \frac{p_{d}}{T} Z_{d}^{-1} + k_{2} \frac{e}{T} Z_{w}^{-1} + k_{3} \frac{e}{T^{2}} Z_{w}^{-1}$$

S	signal path	$p_d$	partial pressure of dry air
n	refractive index	Т	temperature
N	10 <sup>6</sup> ( <i>n</i> -1), refractivity	е	water vapour partial pressure
k <sub>1</sub> , k <sub>2</sub> , k <sub>3</sub>	empirical coefficients	$Z_d, Z_w$	compressibility factors



### Observation modelling in the HIRLAM model

Zenith Total Delay

Interpolation of the model state gives  $ln p_s$  and vertical profiles of T and q at the receiver location

- compressibility factors are assumed unity (hydrostatic balance)
- the profiles are shifted vertically to correspond the receiver height
- ZHD is obtained from In ps
- ZWD is obtained from the numerical integration of q/T in vertical
- ZTD = ZHD + ZWD



# Observation modelling in the HIRLAM model

Slant Total Delay

The first task of the STD modelling algorithm is to determine the signal path

Geometrical

- the satellite azimuth and zenith angles are used
- an explicit correction for the effect of refractive bending

Interpolation of  $In p_s$ , T and q from the model grid to the intersections

- Determination of refractivity at the intersections
- Integration of refractivity along the signal path

Path  $\Delta s_{hor}$   $\lambda s_{k}$   $\Delta z_{k}$ intersection  $\Delta z_{k}$ receiver

Eresmaa and Järvinen, 2006: An observation operator for ground-based GPS slant delays. *Tellus*, **58A**(1), 131-140.



### Observation modelling in the HIRLAM model

#### Slant Total Delay bg-ob statistics



The modelled STD is systematically lower than the observed; especially at large zenith angles

• can be an indicator of incorrect modelling algorithm

Biases are specific for receiver station, but standard deviations are not



# ZTD data assimilation

Near real-time data flow in Europe

Currently more than 500 receiver stations in Europe provide data for ZTD processing

Geodetic processing by more than 10 analysis centres

Drawback: the observations are not consistent with each other, since different analysis centres use different processing strategies!

The geographic distribution of the observations is exceptionally irregular



EUMETNET GPS Water Vapour programme: E-GVAP



# ZTD data assimilation

Impact on Numerical Weather Prediction

Assimilation experiments with ZTD data show neutral to slightly positive impacts on NWP

Problems to be dealt with

- Data quality is inhomogeneous as several analysis centres are processing ZTD with different processing methods
- Observations are *significantly biased*, and the biases are specific for receiver station
- Spatial and temporal *observation error correlations* are difficult to be accounted for



### ZTD data assimilation

Spatial observation error correlation

- ZTD observations show error correlations in *spatial length scales of several hundred km*
- However, application of a proper algorithm for bias correction might eliminate the need for specifying the error correlations!



Eresmaa and Järvinen, 2005: Estimation of spatial GPS Zenith Delay observation error covariance. *Tellus*, **57A**(2), 194-203.



### Further reading

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- de Haan et al., 2004: Synergetic use of GPS water vapour and meteosat images for synoptic weather forecasting. *J. Appl. Meteorol.*, **43**, 514-518.
- Elgered et al., 2005: COST Action 716 Exploitation of ground-based GPS for operational numerical weather prediction and climate applications. Final report. 234 pp.
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